

Cloud working week

16-18 January 2017, Toulouse, France



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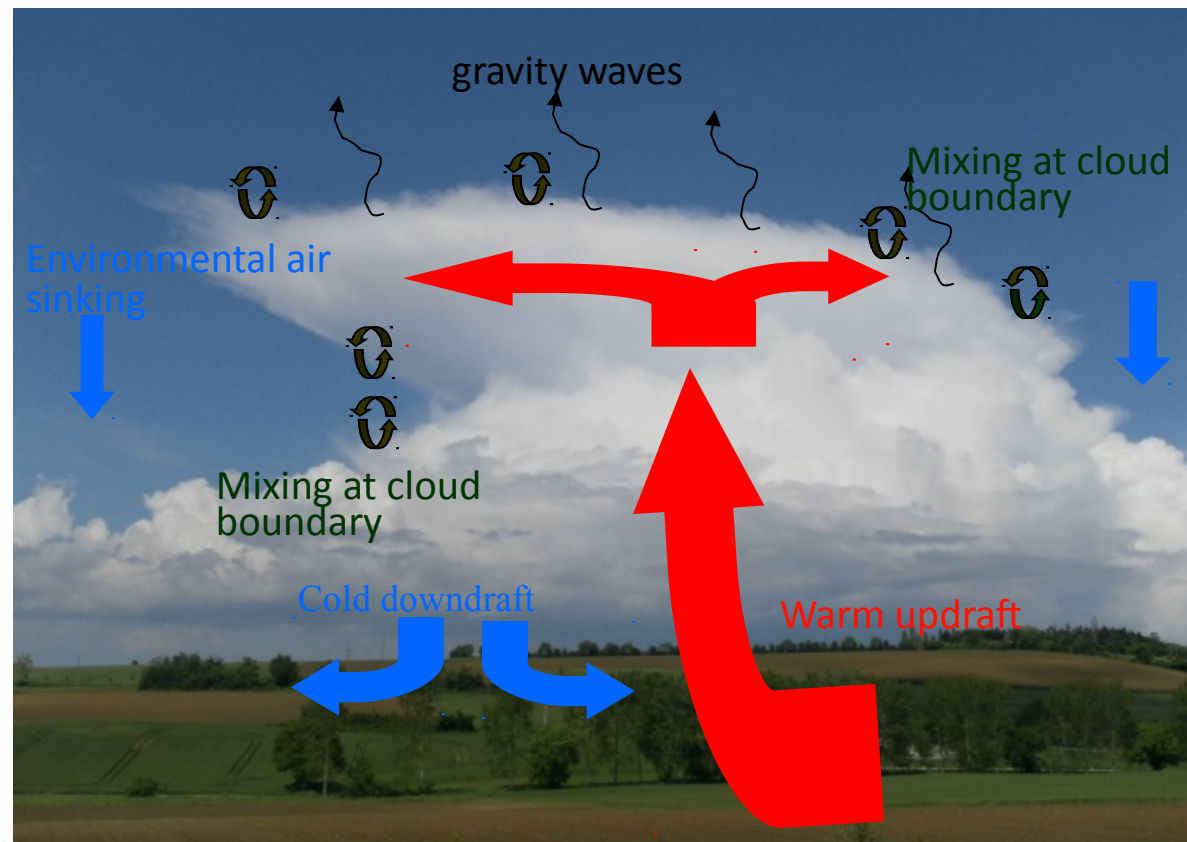
Representation of turbulence in simulations of deep convective clouds

Introduction

Turbulence: studied extensively in the atmospheric boundary layer

Convective clouds associated with **strong turbulence**: instabilities, updraft, downdraft, gravity waves ...

- 1 - Idealized **Large-Eddy Simulations** of deep convection with the Meso-NH model
- 2 - Characterization of **turbulence** inside convective clouds
- 3 - Evaluation and improvement of **turbulence parameterization**



1 - LES of deep convective clouds

Configuration with Meso-NH:

1.5 order turbulence scheme:
pronostic TKE (Cuxart et al. 2000)
with Deardorff mixing length

one-moment microphysical scheme
ICE3 (ice, cloud water, graupel, snow,rain)

no radiation scheme

no Coriolis force

surface fluxes: H, LE

1 - LES of deep convective clouds

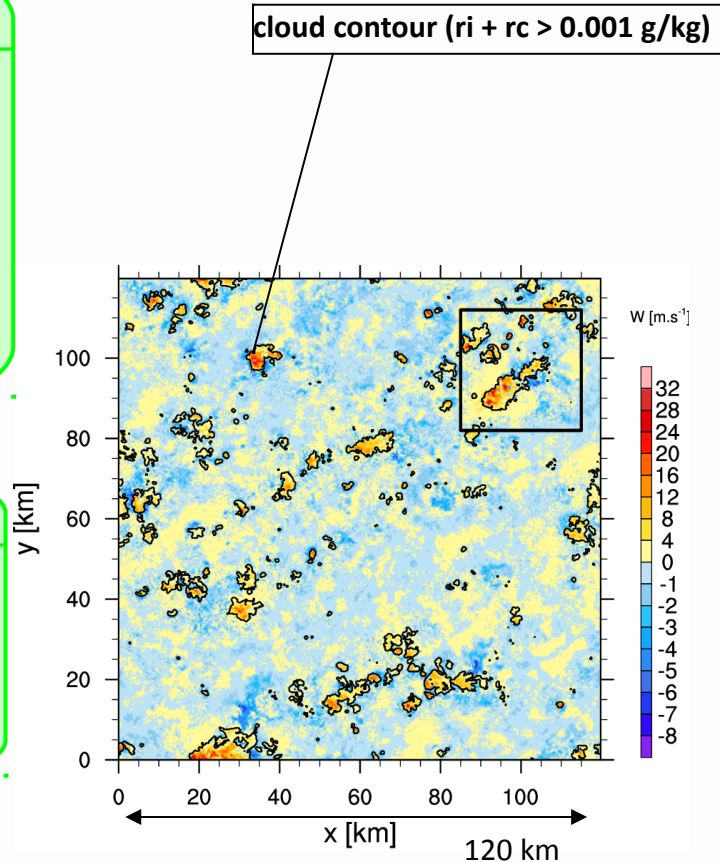
Horizontal cross section of vertical velocities (m/s) at 6 km AGL t= 175 min

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Initial conditions:

Unstable conditions from idealized
profiles Weisman and Klemm (1982)
Moderate vertical wind shear
White noise on low-level θ



$\Delta x, \Delta y = 200\text{m}$ $\Delta z = 50\text{m}$

600x600 points x 293 levels
~105 millions points

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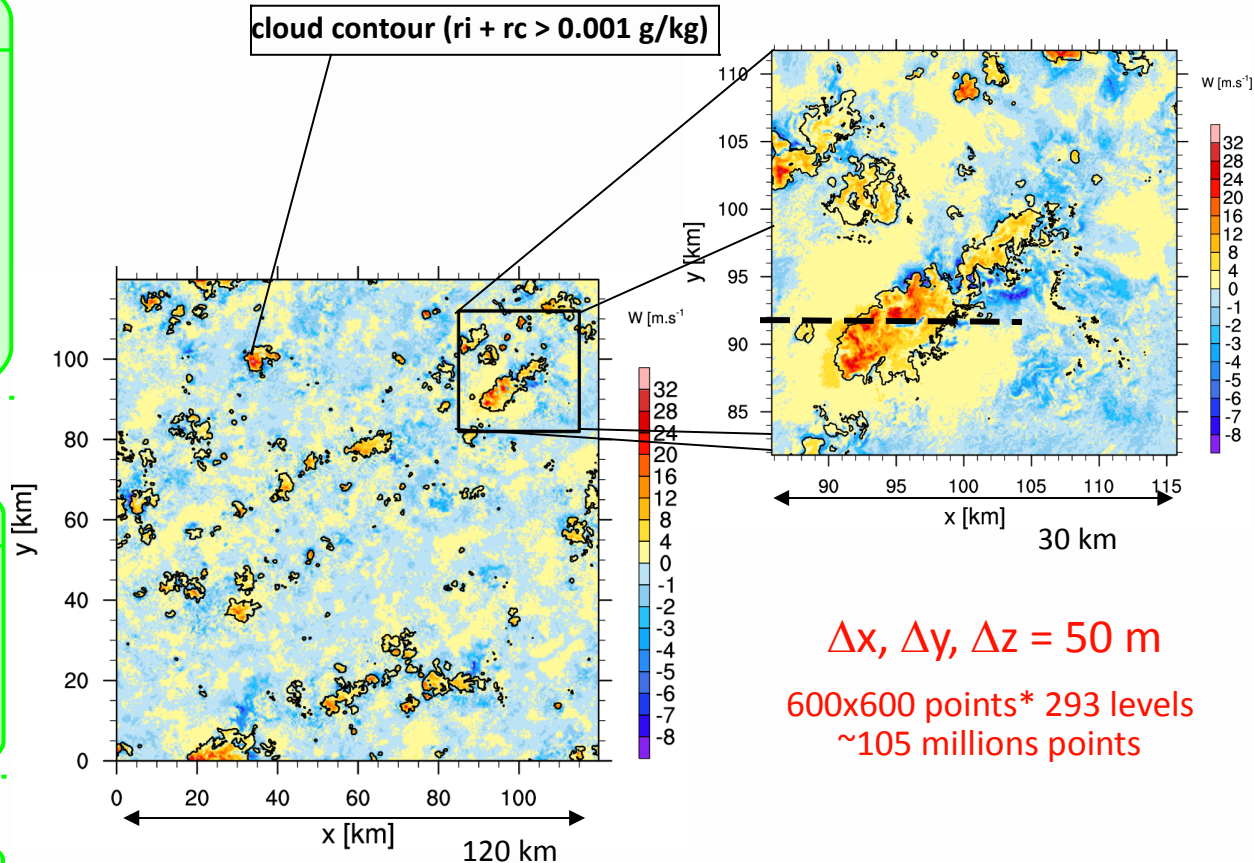
Initial conditions:

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White noise on low-level θ

Grid-nesting configuration:

2 domains (one-way nesting)

Horizontal cross section of vertical velocities (m/s) at 6 km AGL t= 175 min



$\Delta x, \Delta y, \Delta z = 50$ m

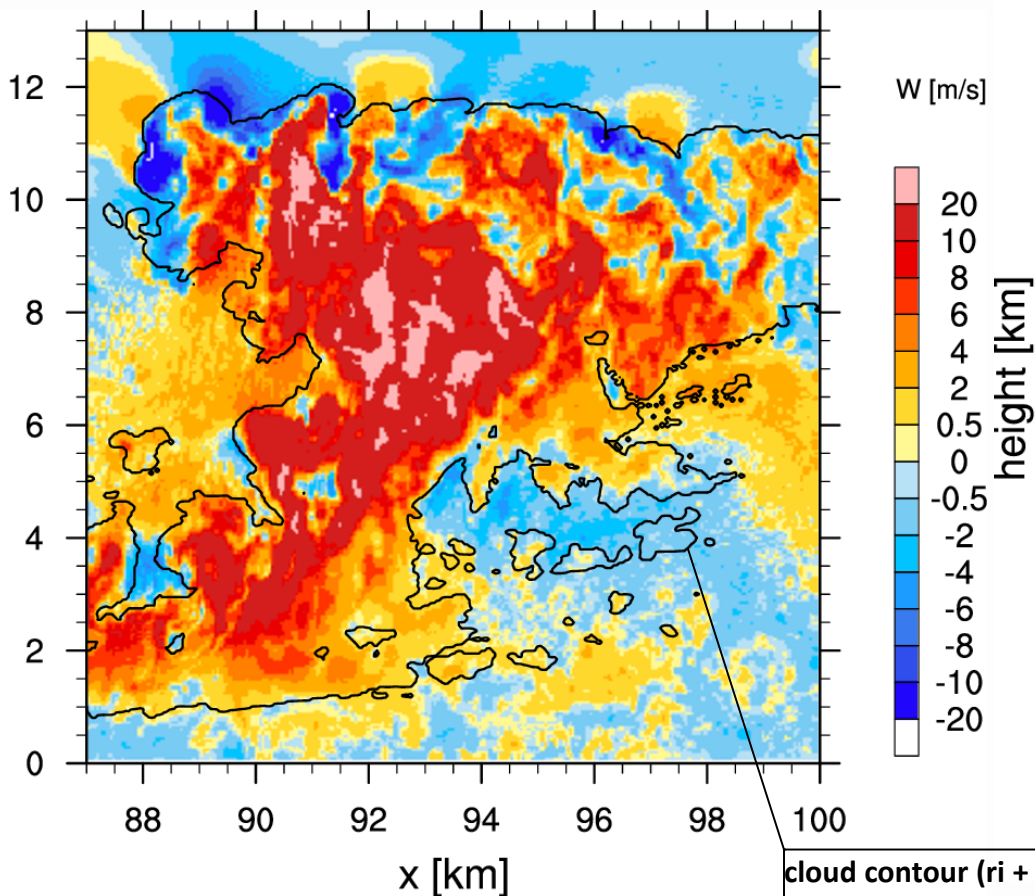
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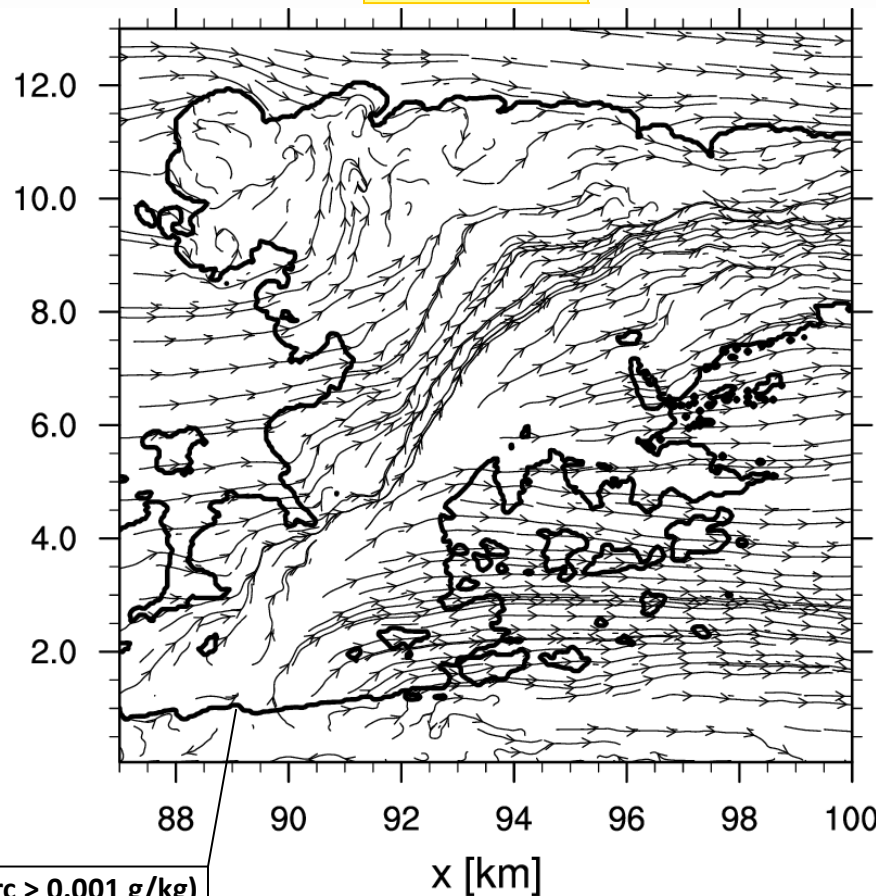
600x600 points x 293 levels
~105 millions points

1 - LES of deep convective clouds

Vertical cross sections at 175 min: W (m/s)



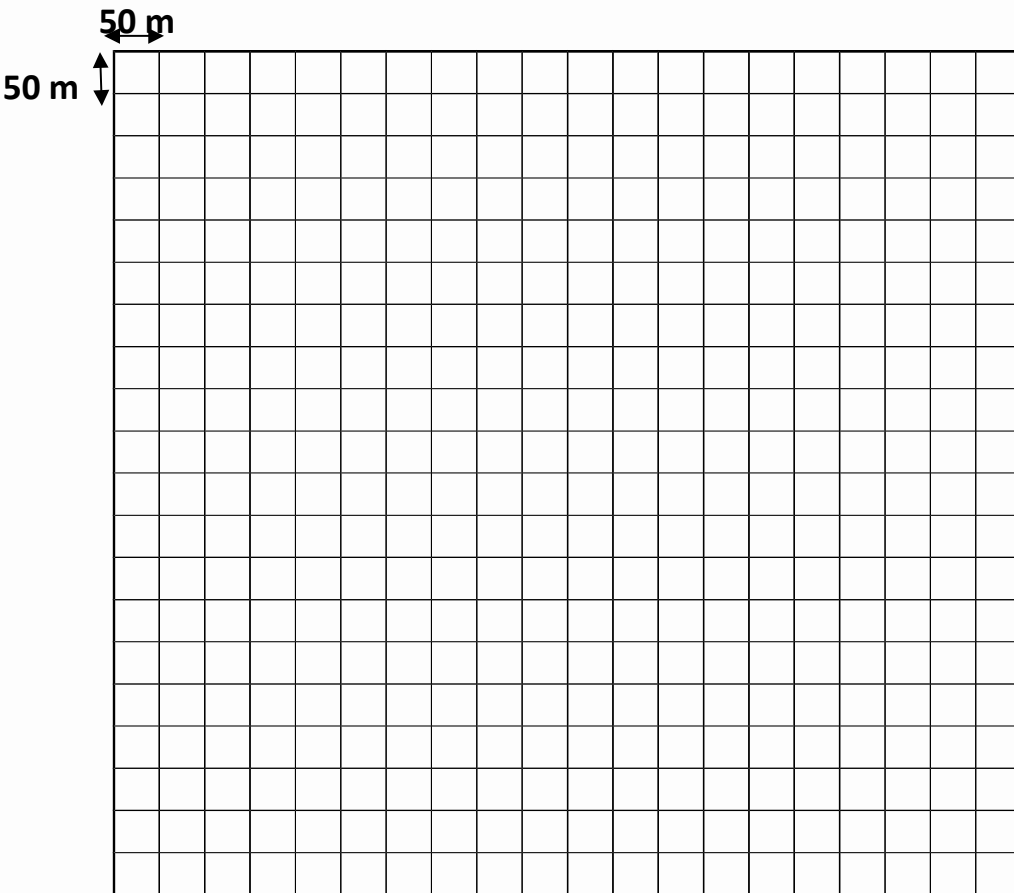
Streamlines



→ well-developed cumulonimbus with a strong updraft and many eddies

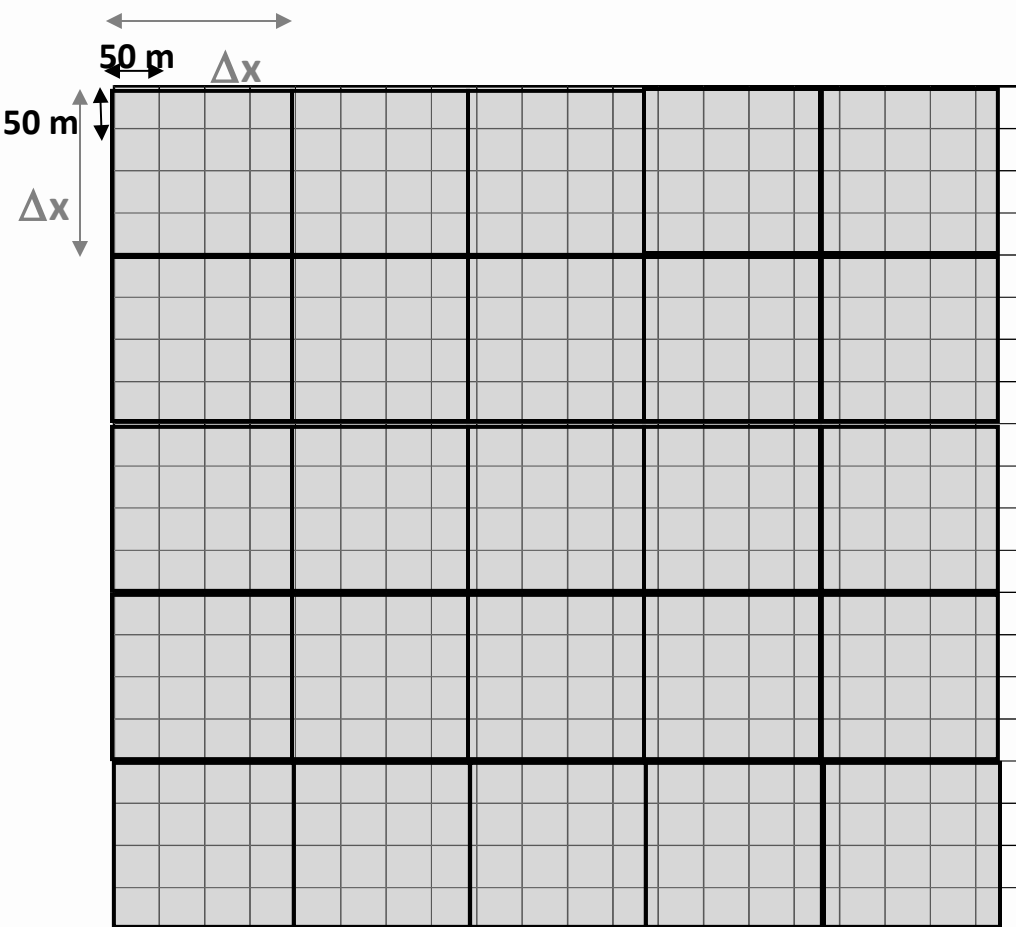
2 – Characterization of turbulence inside convective clouds

- LES: reference simulation (50-m grid spacing)



2 – Characterization of turbulence inside convective clouds

- LES: reference simulation (50-m grid spacing)
- Computation of reference fields at coarser resolutions Δx (500m, 1 km, 2 km) by averaging LES fields
- Mean filtering by boxes of size Δx (Honnert et al. 2011, Shin and Hong, 2013, Moeng 2014 ...)

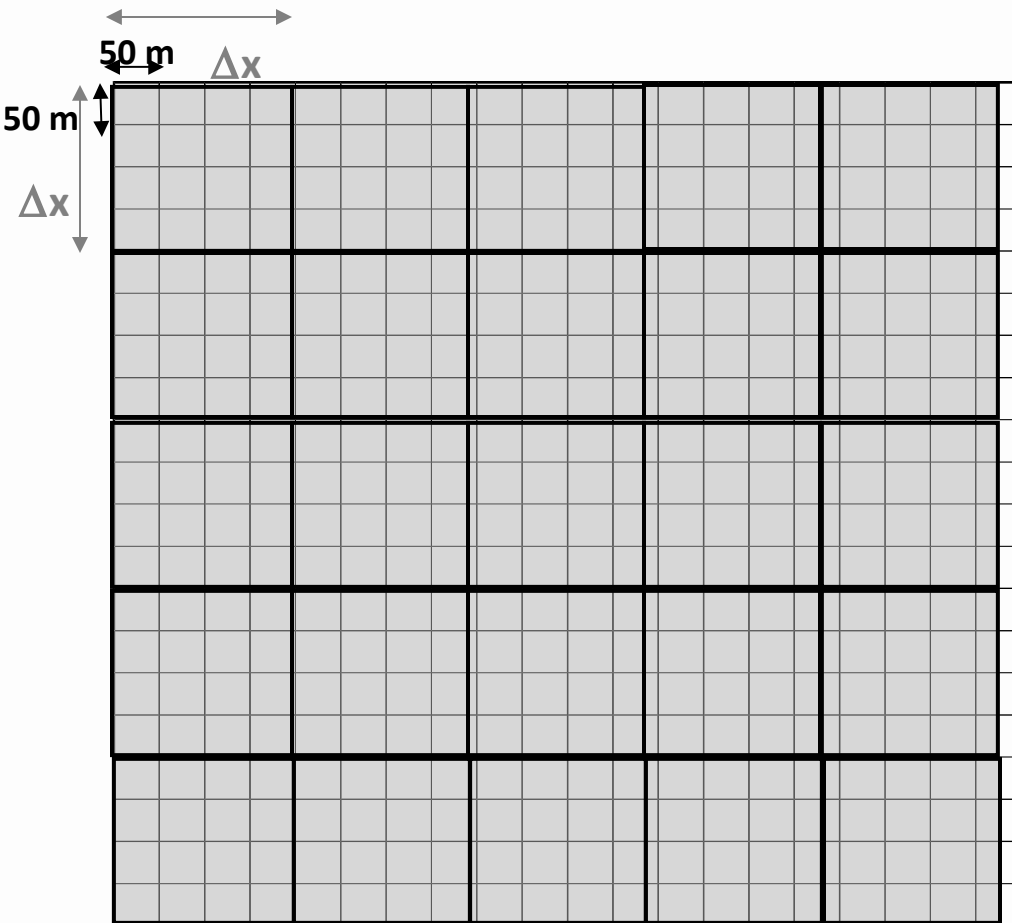


Computation of terms at Δx :

$$\overline{u}^{\Delta x}, \overline{v}^{\Delta x}, \overline{w}^{\Delta x}, \overline{r_{np}}^{\Delta x}, \overline{\theta_l}^{\Delta x}, \dots$$

2 – Characterization of turbulence inside convective clouds

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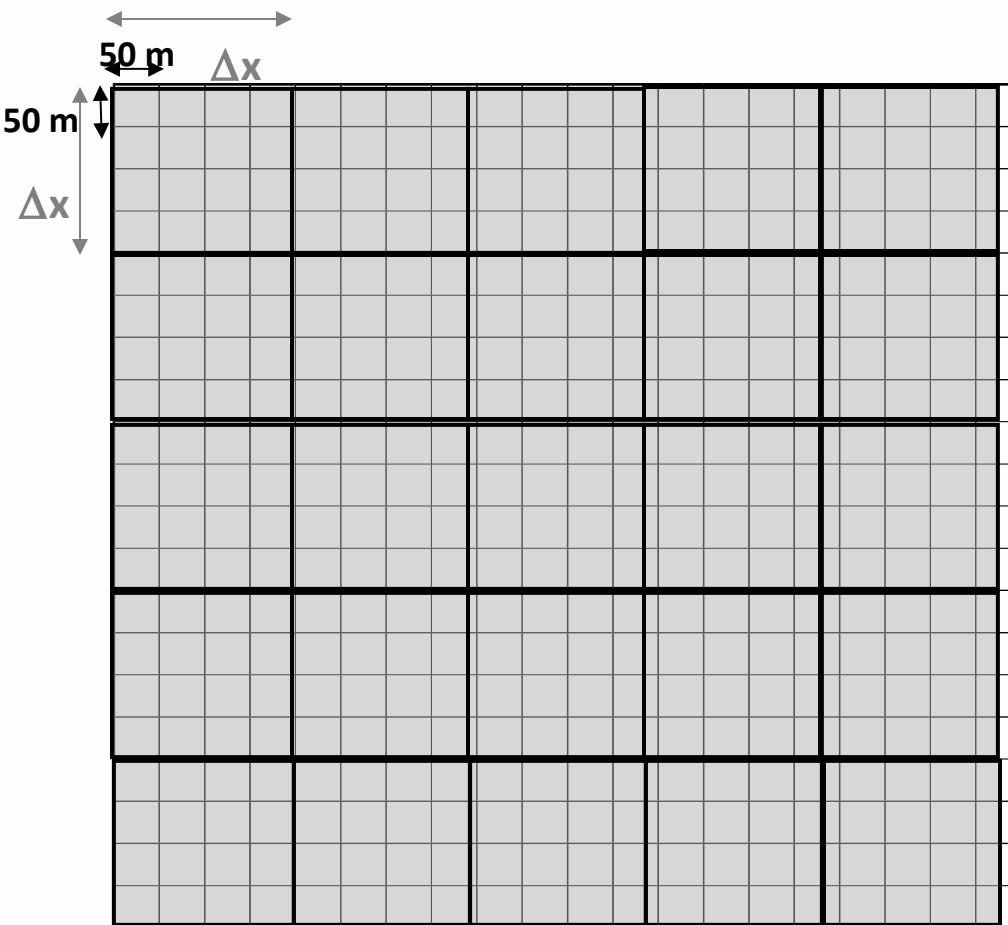
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$$u'_i = (u_i - \overline{u_i}^{\Delta x})$$

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$$u'_i = (u_i - \overline{u}_i^{\Delta x})$$

Computation of subgrid terms at Δx :

- turbulent fluxes:

$$\overline{u'v'}^{\Delta x}, \overline{u'w'}^{\Delta x}, \overline{v'w'}^{\Delta x}, \overline{w'r'_{np}}^{\Delta x}, \overline{w'\theta'_l}^{\Delta x}, \dots$$

$$\overline{u'_i u'_j}^{\Delta x} = \overline{(u_i - \overline{u}_i^{\Delta x})(u_j - \overline{u}_j^{\Delta x})}^{\Delta x} + f^{u'_i u'_j}^{\Delta x}$$

- variances:

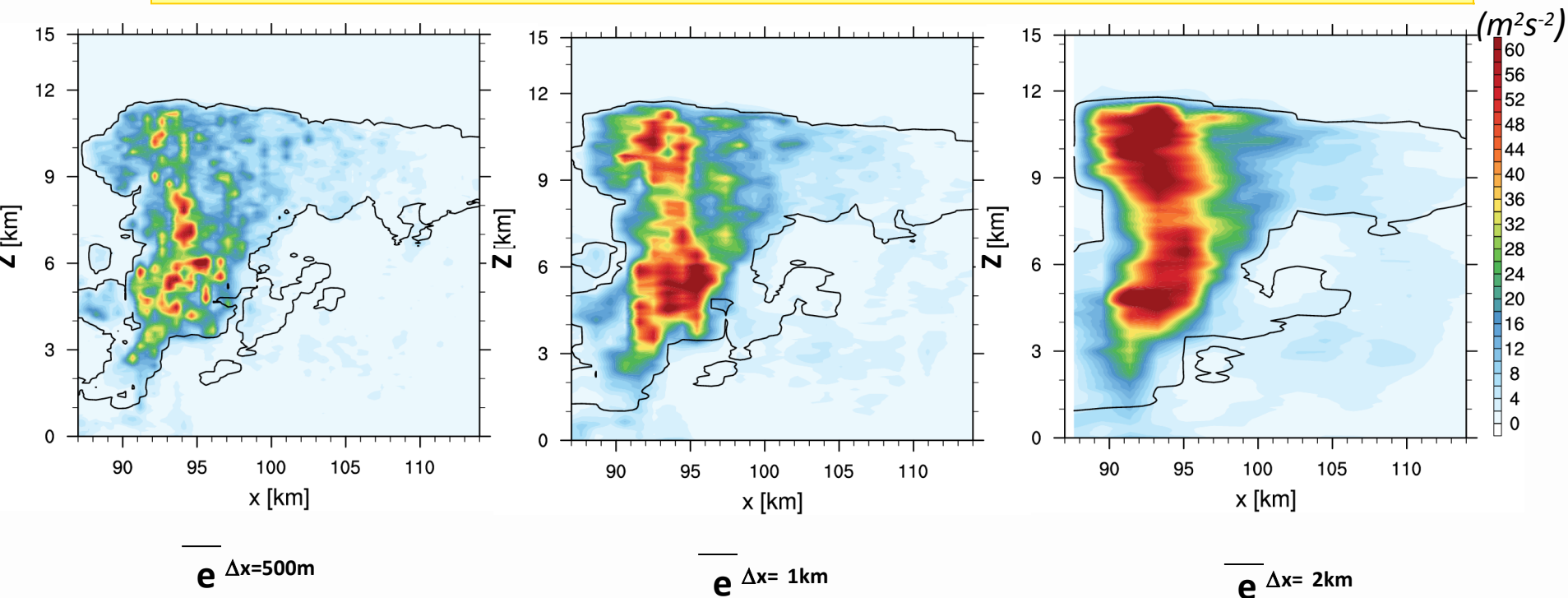
$$\overline{u'^2}^{\Delta x}, \overline{v'^2}^{\Delta x}, \overline{w'^2}^{\Delta x}, \overline{r'^2_{np}}^{\Delta x}, \overline{\theta_l'^2}^{\Delta x}, \dots$$

-TKE:

$$\overline{e}_{ref}^{\Delta x} = \frac{1}{2}(\overline{u'^2}^{\Delta x} + \overline{v'^2}^{\Delta x} + \overline{w'^2}^{\Delta x})$$

2 – Characterization of turbulence inside convective clouds

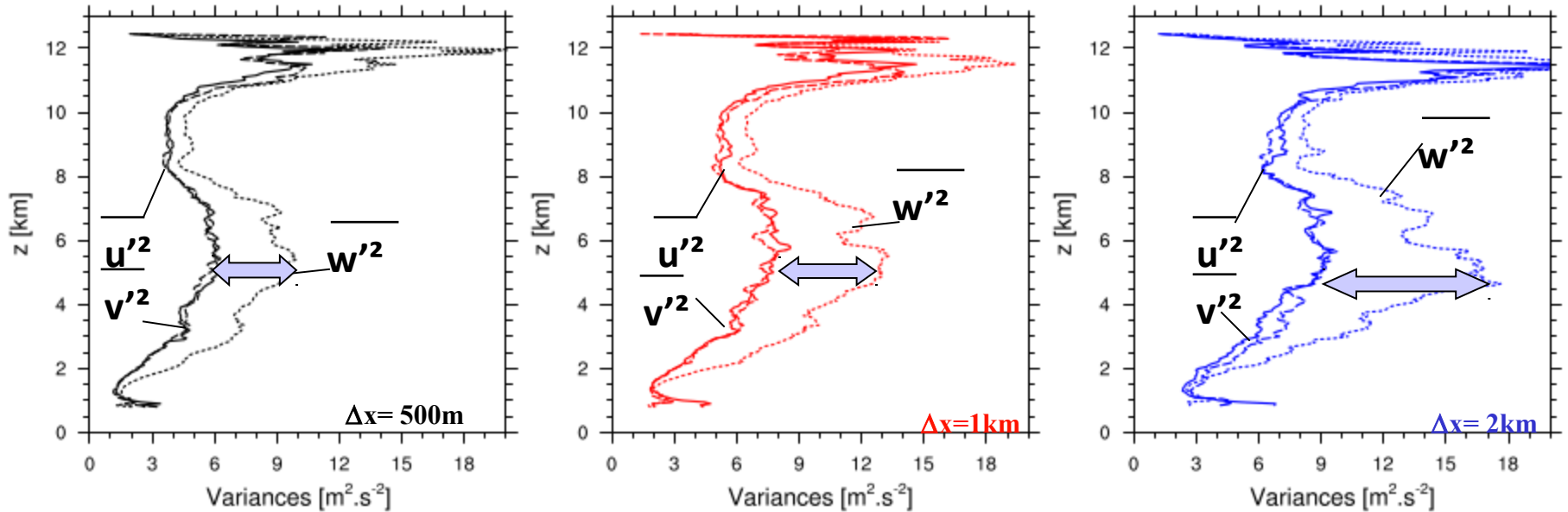
Vertical cross sections: TKE for different Δx (500m, 1 km, 2 km) from LES at t= 175 min



- strong turbulence inside the cloud
- subgrid TKE increases with coarser resolutions

2 – Characterization of turbulence inside convective clouds

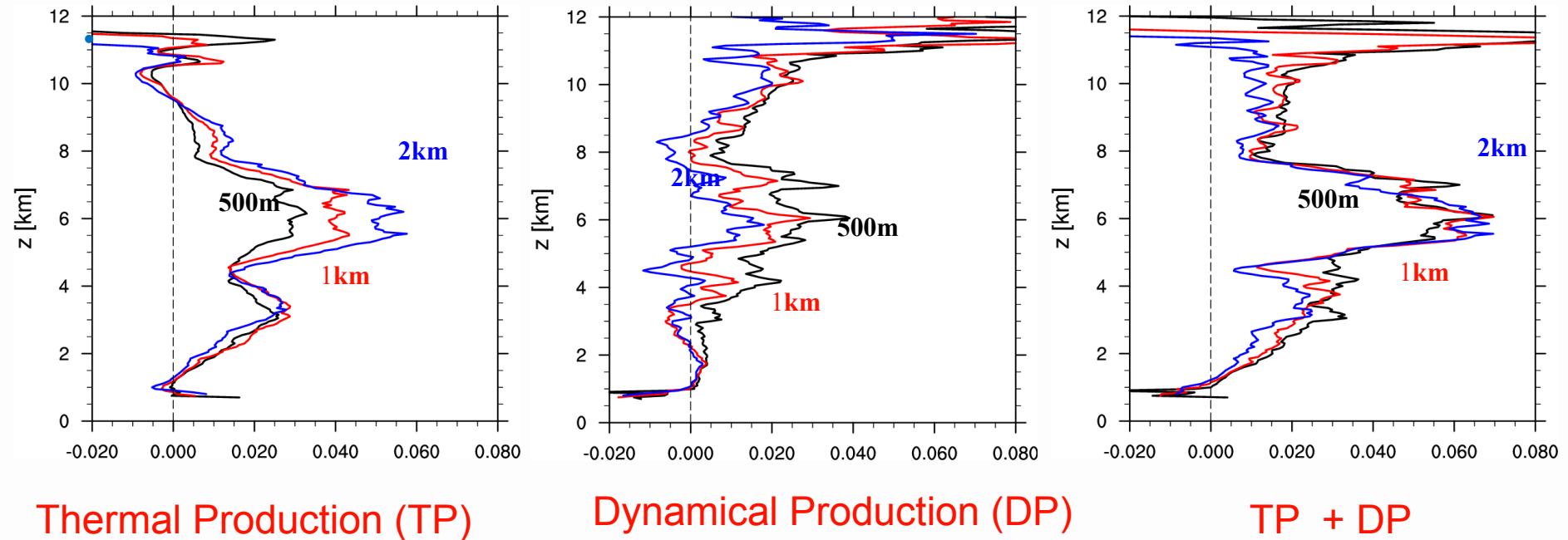
Vertical profiles: wind variances for different Δx (500m, 1 km, 2 km) from LES at t= 175 min



- variance of w is greater than variances of u and v : anisotropy
- anisotropy increases with coarser resolutions

2 – Characterization of turbulence inside convective clouds

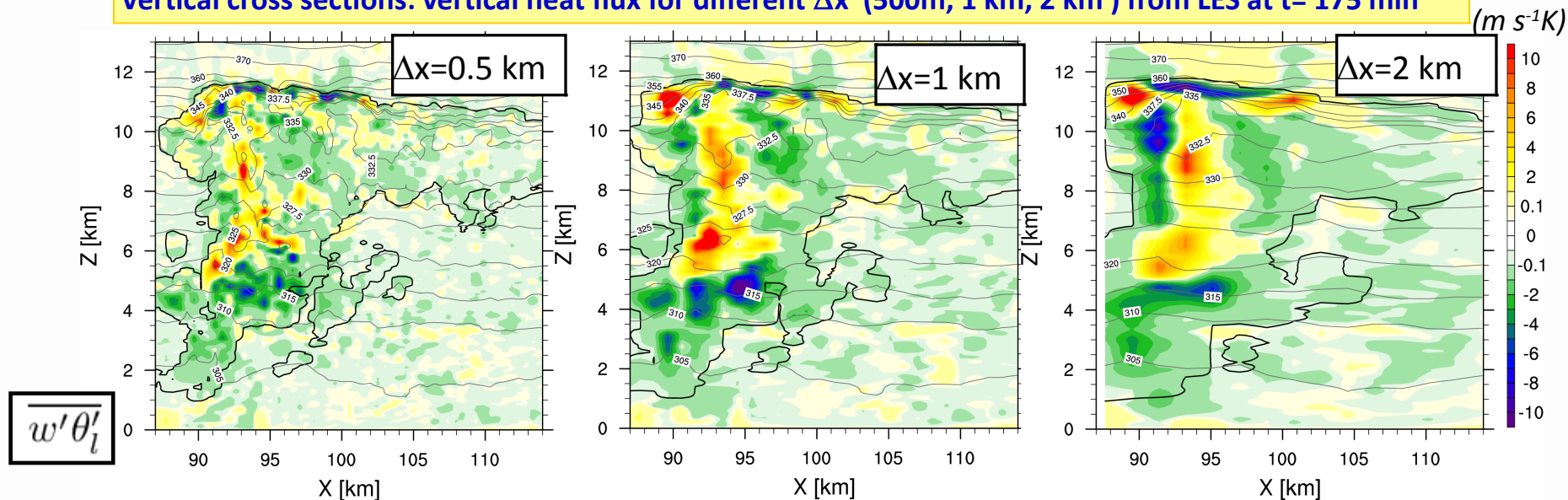
Vertical profiles: subgrid thermal and dynamical productions (m^2/s^3) for different Δx $t= 175$ min



- TP increases with coarser resolutions: 500m \rightarrow 1km \rightarrow 2km
- DP decreases with coarser resolutions (horizontal gradients)
- Sum seems quite similar (compensation between DP and TP?)

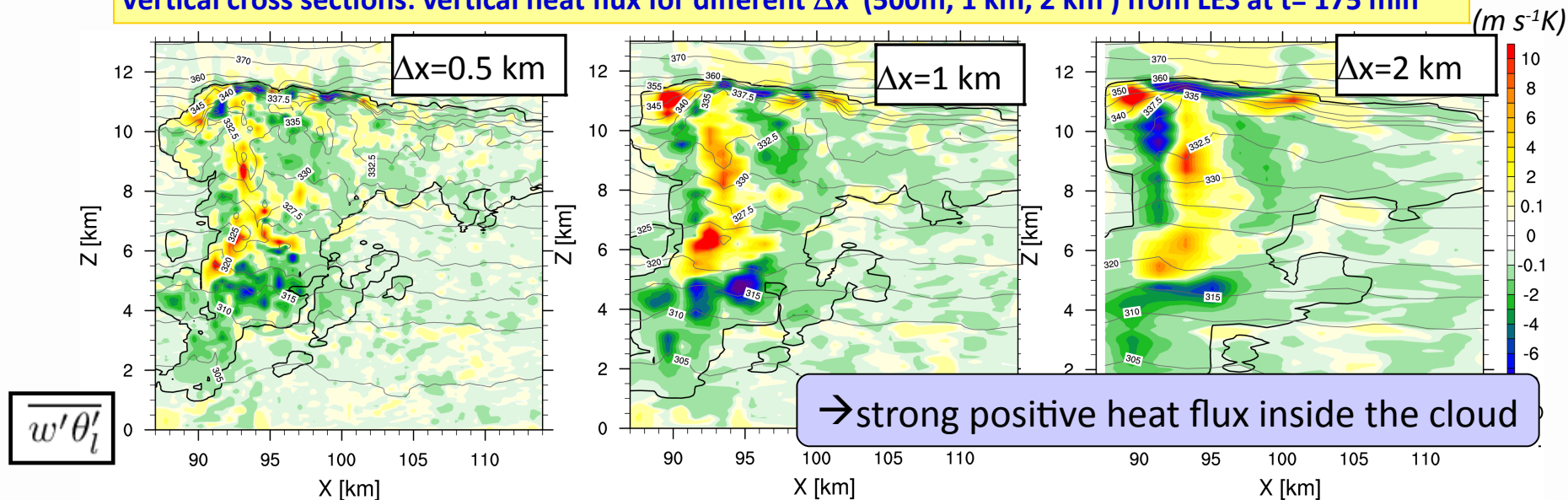
2 – Characterization of turbulence inside convective clouds

Vertical cross sections: vertical heat flux for different Δx (500m, 1 km, 2 km) from LES at t= 175 min



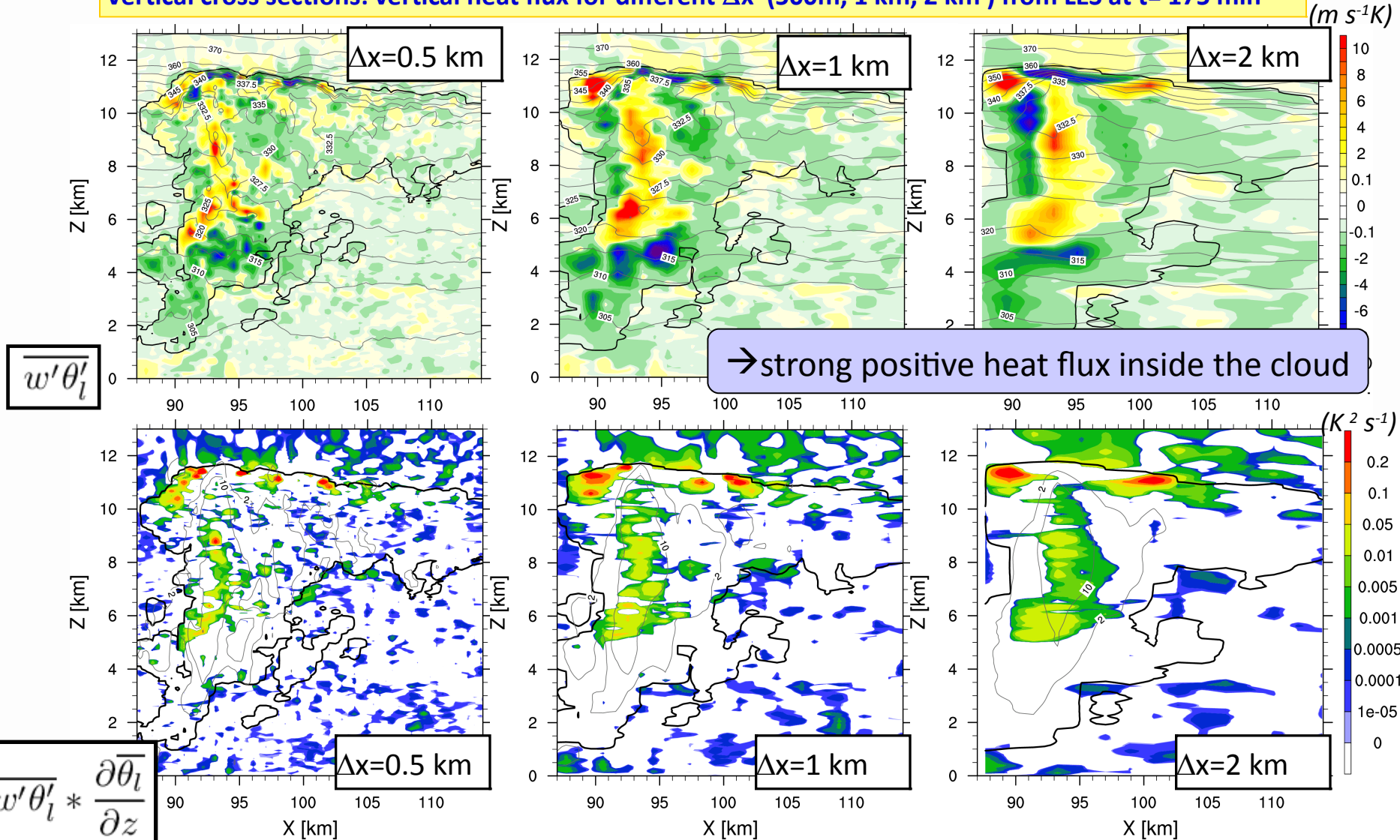
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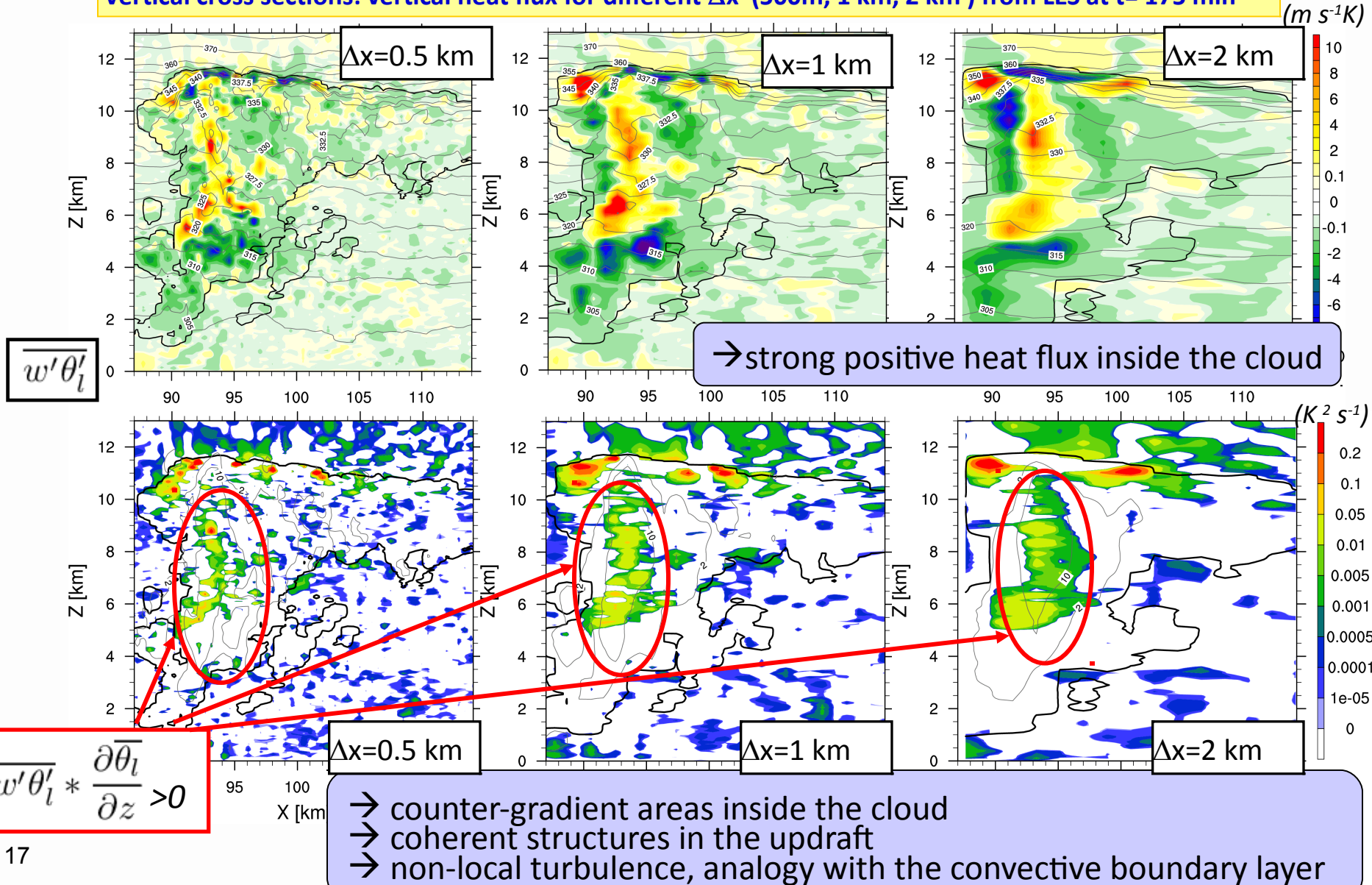
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Vertical cross sections: vertical heat flux for different Δx (500m, 1 km, 2 km) from LES at t= 175 min



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Vertical cross sections: vertical heat flux for different Δx (500m, 1 km, 2 km) from LES at t= 175 min



3 – Evaluation of turbulence parameterization

Off-line evaluation: computation of parameterized fluxes from LES at $\Delta x \rightarrow \overline{w'\theta'_l}$

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Kgrad

Cuxart et al (2000)

$$\overline{w'\theta'_l}^{\Delta x} = -\frac{2}{3C_{p\theta}} \overline{\phi_i}^{\Delta x} L \sqrt{\overline{e}_{ref}^{\Delta x}} \frac{\partial \overline{\theta}_l^{\Delta x}}{\partial z}$$

based on K-gradient: $\overline{w'\theta'_l} = -K \frac{\partial \overline{\theta}_l}{\partial z}$

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Off-line evaluation: computation of parameterized fluxes from LES at $\Delta x \rightarrow \overline{w'\theta'_l}$

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Hgrad

Moeng et al (2010)

$$\overline{w'\theta'_l}^{\Delta x} = C_{\Delta x} \left(\frac{\partial \overline{w}^{\Delta x}}{\partial x} \frac{\partial \overline{\theta_l}^{\Delta x}}{\partial x} + \frac{\partial \overline{w}^{\Delta x}}{\partial y} \frac{\partial \overline{\theta_l}^{\Delta x}}{\partial y} \right)$$

based on horizontal gradients: $\overline{w'\theta'_l} = C \left(\frac{\partial \overline{w}}{\partial x} \frac{\partial \overline{\theta_l}}{\partial x} + \frac{\partial \overline{w}}{\partial y} \frac{\partial \overline{\theta_l}}{\partial y} \right)$

related to a mass flux (Moeng, 2014)

3 – Evaluation of turbulence parameterization

Off-line evaluation: computation of parameterized fluxes from LES at $\Delta x \rightarrow \overline{w'r'_{np}}$

Kgrad

Cuxart et al (2000)

$$\overline{w'r'_{np}}^{\Delta x} = -\frac{2}{3C_{pr}} \overline{\phi_i}^{\Delta x} L \sqrt{\overline{e}_{ref}^{\Delta x}} \frac{\partial \overline{r_{np}}^{\Delta x}}{\partial z}$$

based on K-gradient: $\overline{w'r'_{np}} = -K \frac{\partial \overline{r_{np}}}{\partial z}$

Hgrad

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$$\overline{w'r'_{np}}^{\Delta x} = C_{\Delta x} \left(\frac{\partial \overline{w}^{\Delta x}}{\partial x} \frac{\partial \overline{r_{np}}^{\Delta x}}{\partial x} + \frac{\partial \overline{w}^{\Delta x}}{\partial y} \frac{\partial \overline{r_{np}}^{\Delta x}}{\partial y} \right)$$

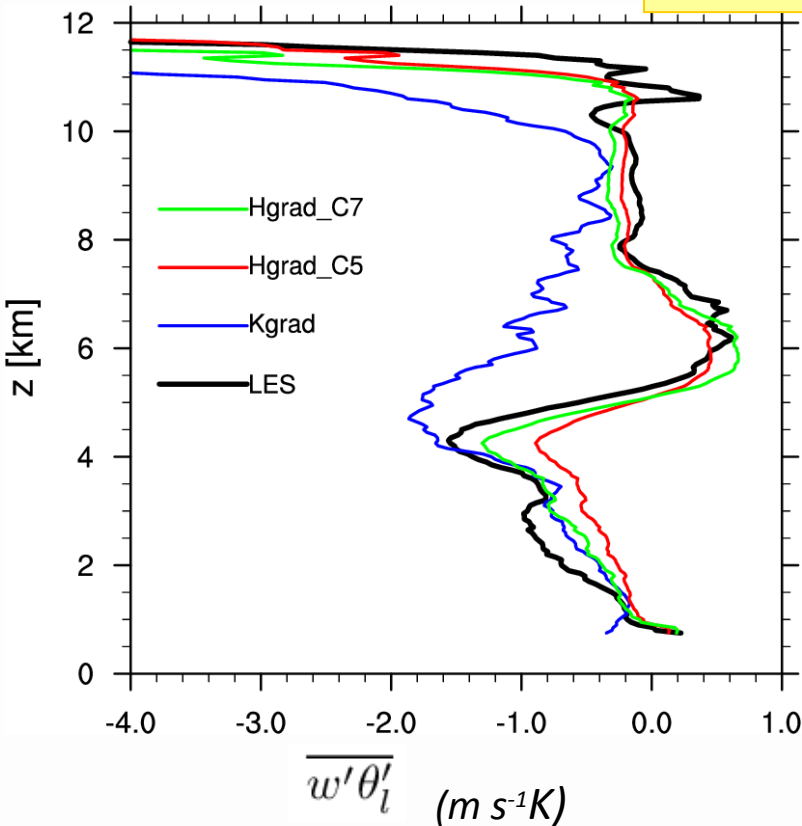
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3 – Evaluation of turbulence parameterization

Off-line evaluation: using LES fields filtered at $\Delta x = 1$ km

Vertical profiles inside convective system $t = 175$ min



REF (LES)

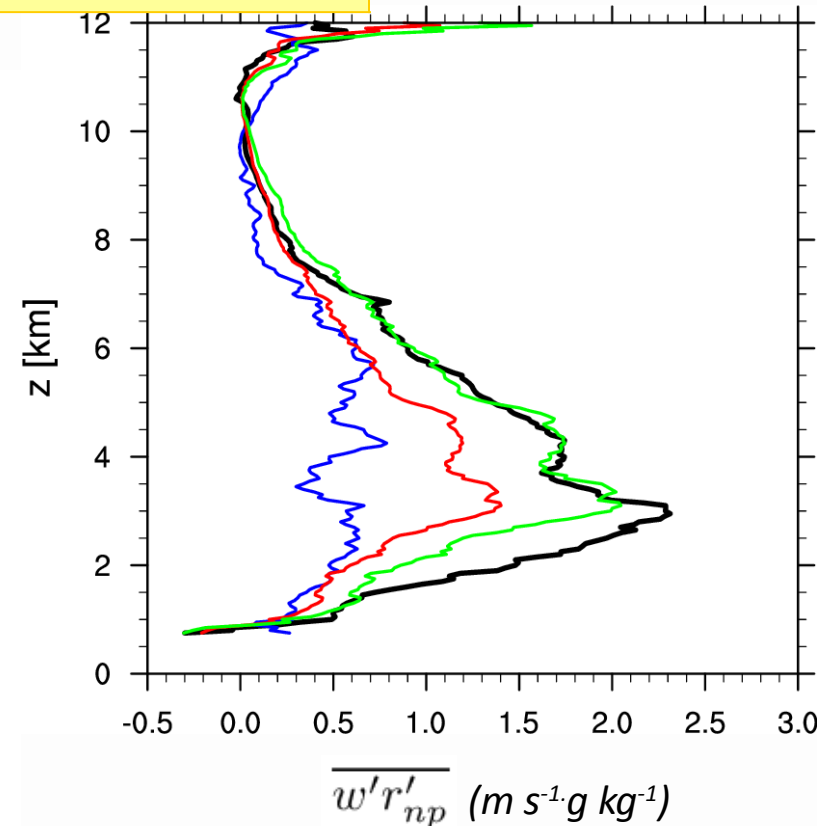
Kgrad

Hgrad

$C = 5\Delta x^2/12$

Hgrad

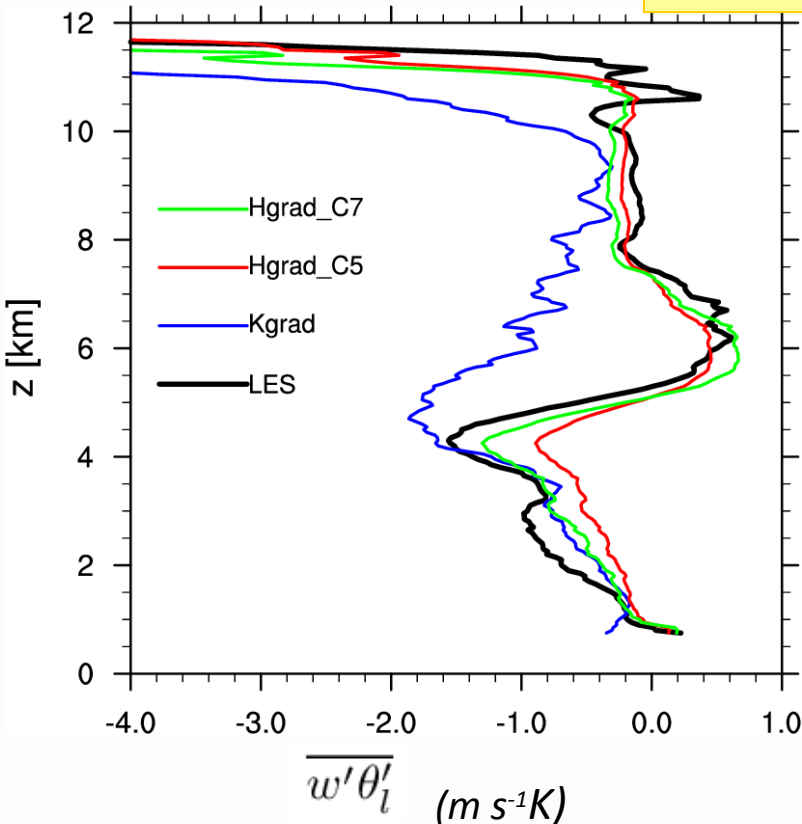
$C = 7\Delta x^2/12$



3 – Evaluation of turbulence parameterization

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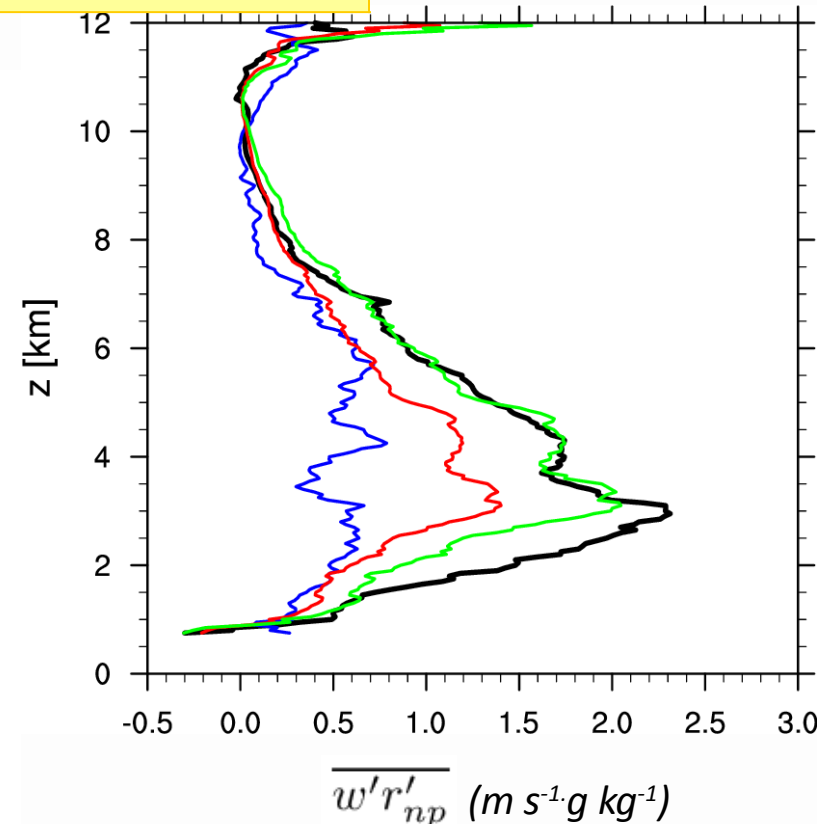
Kgrad

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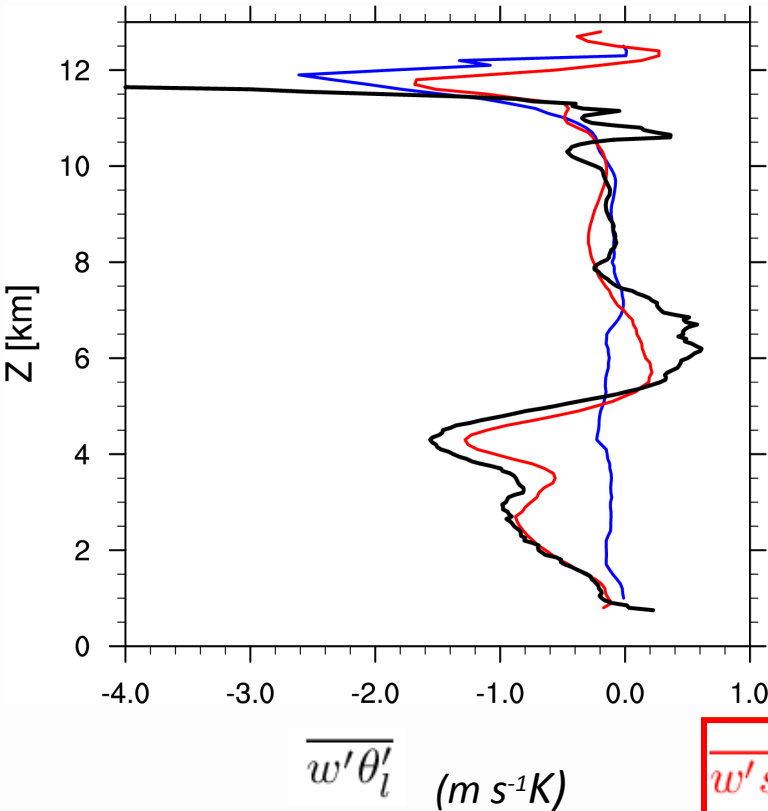


- Kgrad underestimates these two fluxes compared to REF
- Hgrad increases the fluxes and represents positive $w'\theta'_l$ in mid-troposphere

3 – Evaluation of turbulence parameterization

On-line evaluation: simulations with $\Delta x = 1$ km

Vertical profiles inside convective system $t = 180$ min



REF (LES)

Kgrad

$$\overline{w's'} = -K \frac{\partial \bar{s}}{\partial z}$$

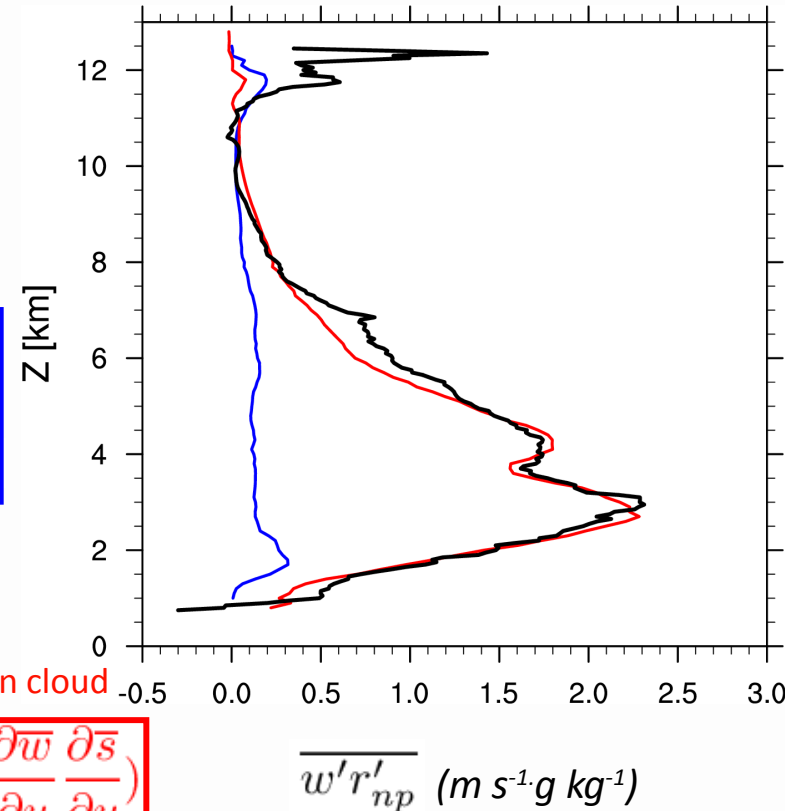
$$s = r_{np}, \theta_l$$

Hgrad

applied only in cloud

$$\overline{w's'} = C \left(\frac{\partial \bar{w}}{\partial x} \frac{\partial \bar{s}}{\partial x} + \frac{\partial \bar{w}}{\partial y} \frac{\partial \bar{s}}{\partial y} \right)$$

$$(C = 3\Delta x^2/12) \quad s = r_{np}, \theta_l$$

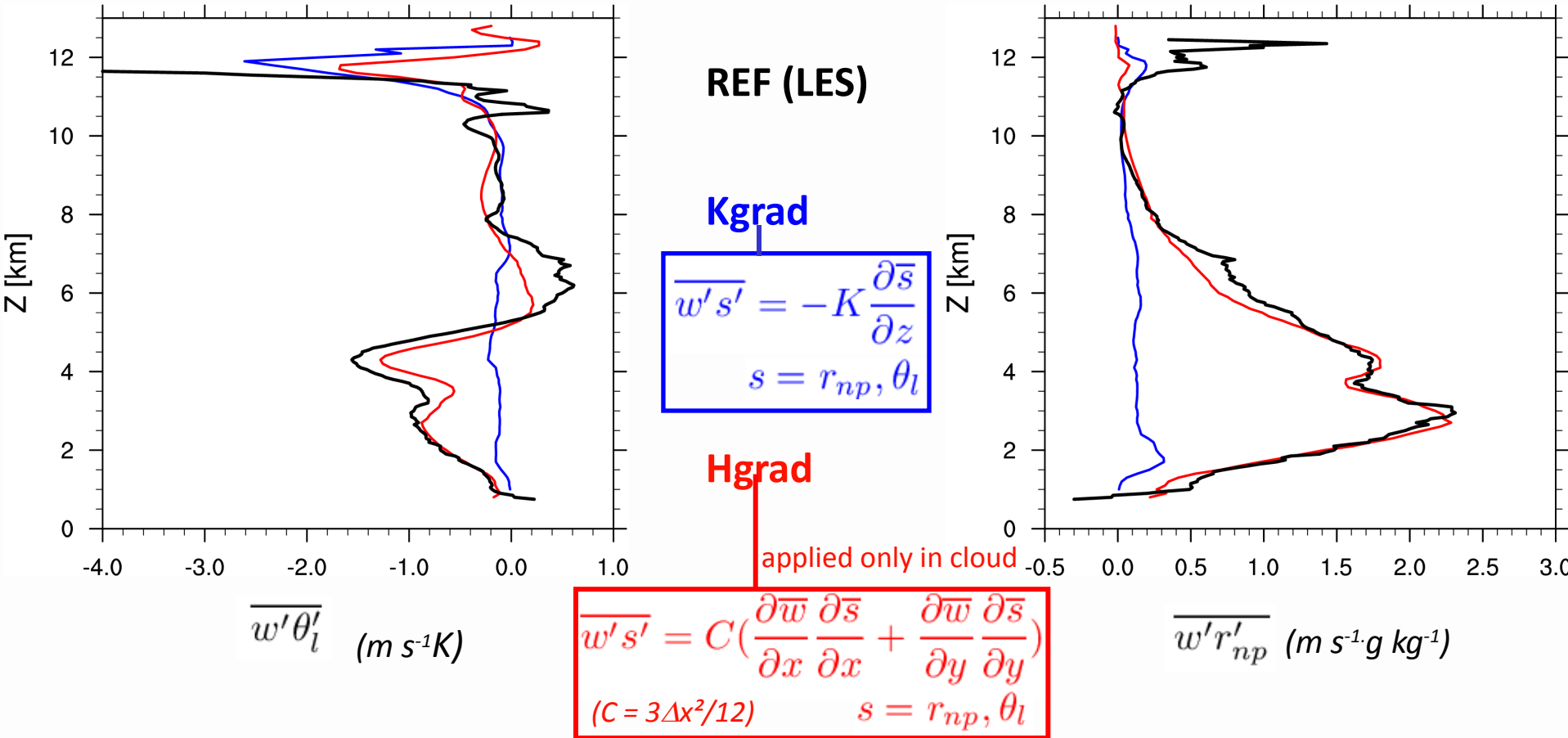


$\overline{w'r'_{np}}$ (m s⁻¹g kg⁻¹)

3 – Evaluation of turbulence parameterization

On-line evaluation: simulations with $\Delta x = 1$ km

Vertical profiles inside convective system $t = 180$ min

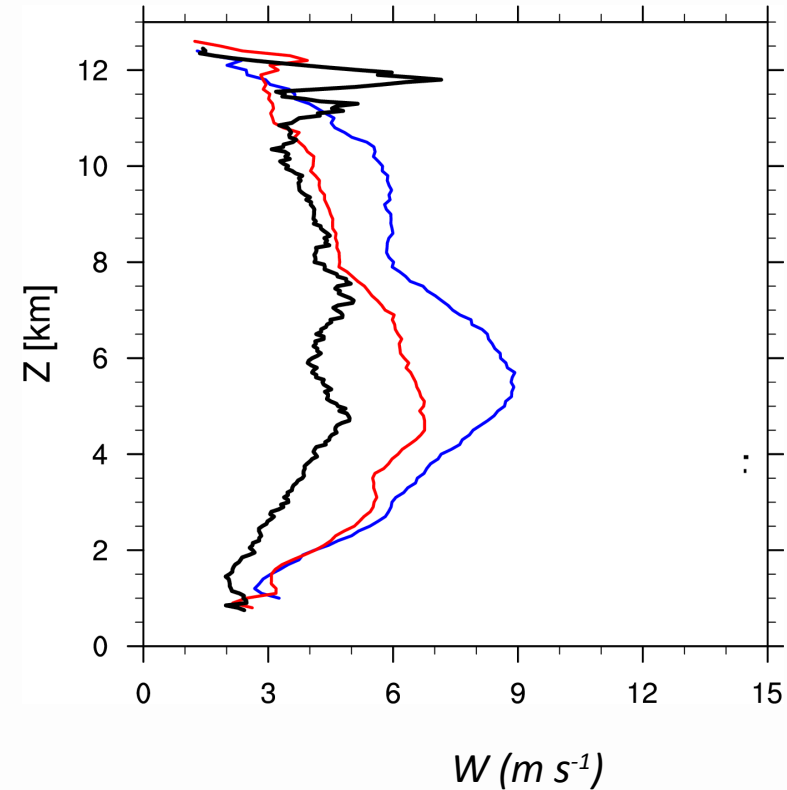
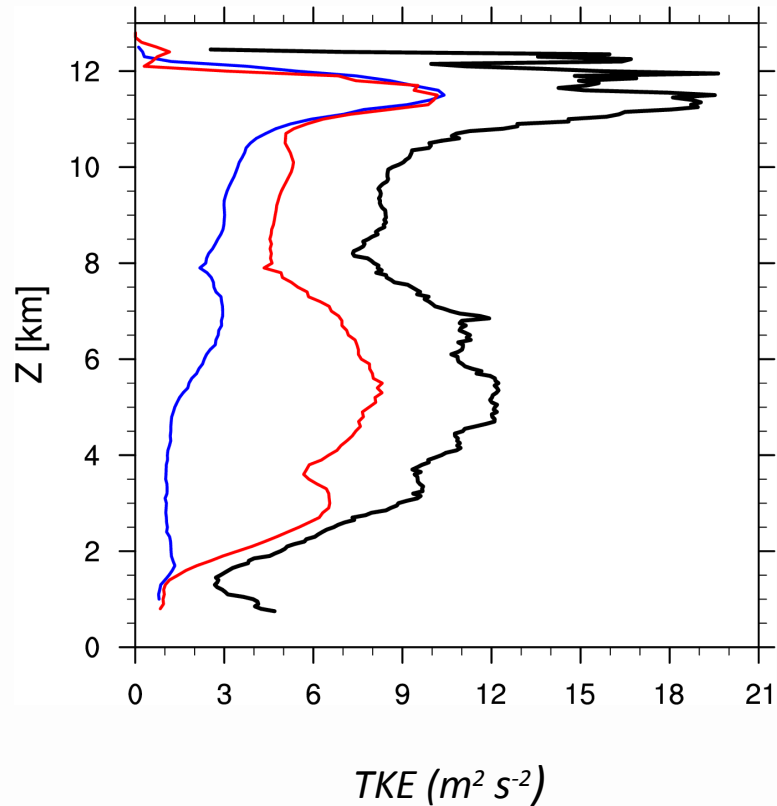


→ better representation of those vertical turbulent fluxes with **Hgrad**

3 – Evaluation of turbulence parameterization

On-line evaluation: simulations with $\Delta x = 1$ km

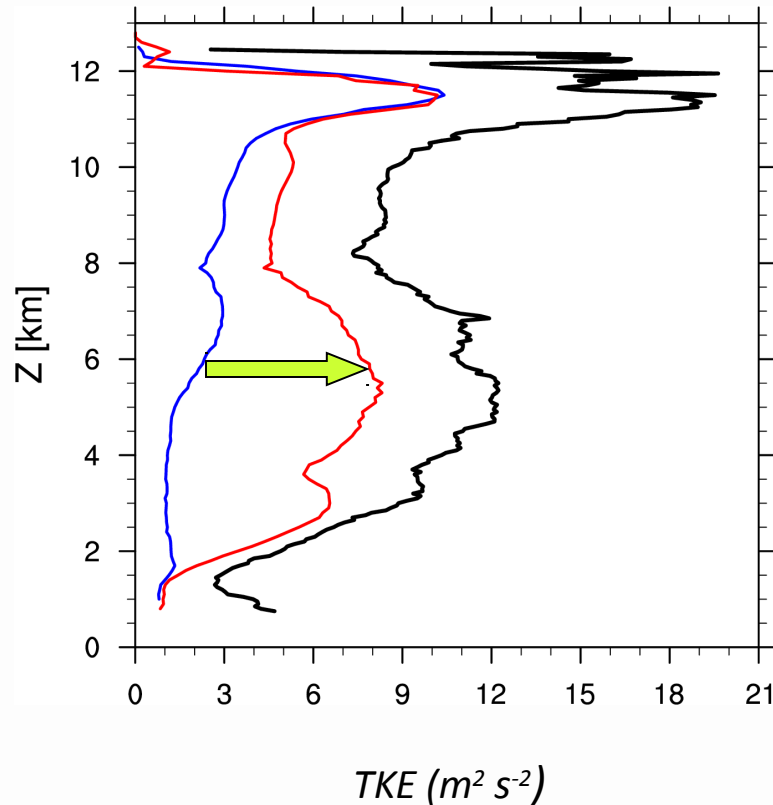
Vertical profiles inside convective system t= 180 min



3 – Evaluation of turbulence parameterization

On-line evaluation: simulations with $\Delta x = 1$ km

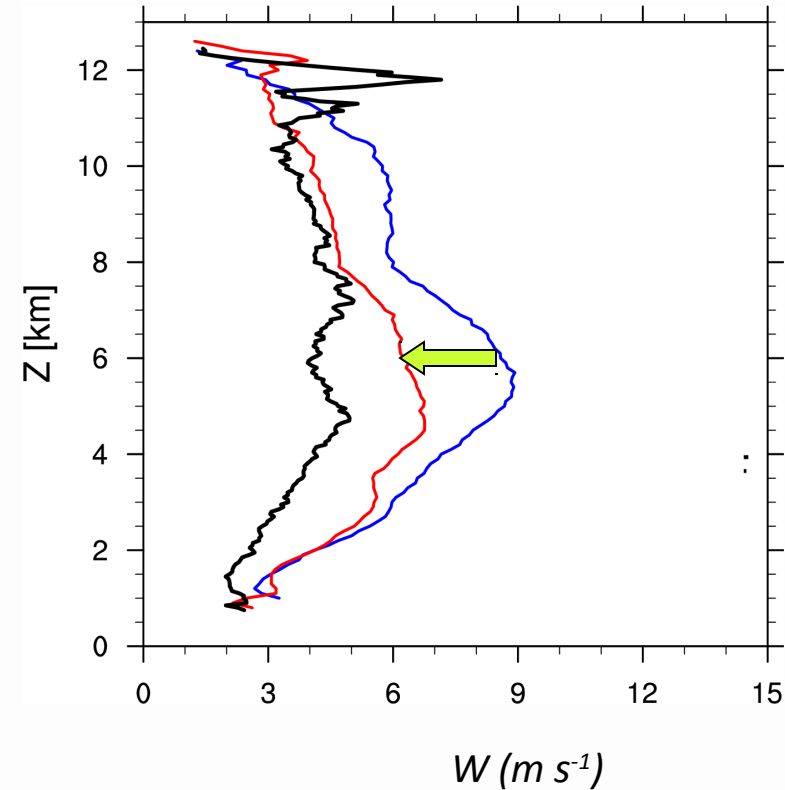
Vertical profiles inside convective system $t = 180$ min



REF (LES)

Kgrad

Hgrad

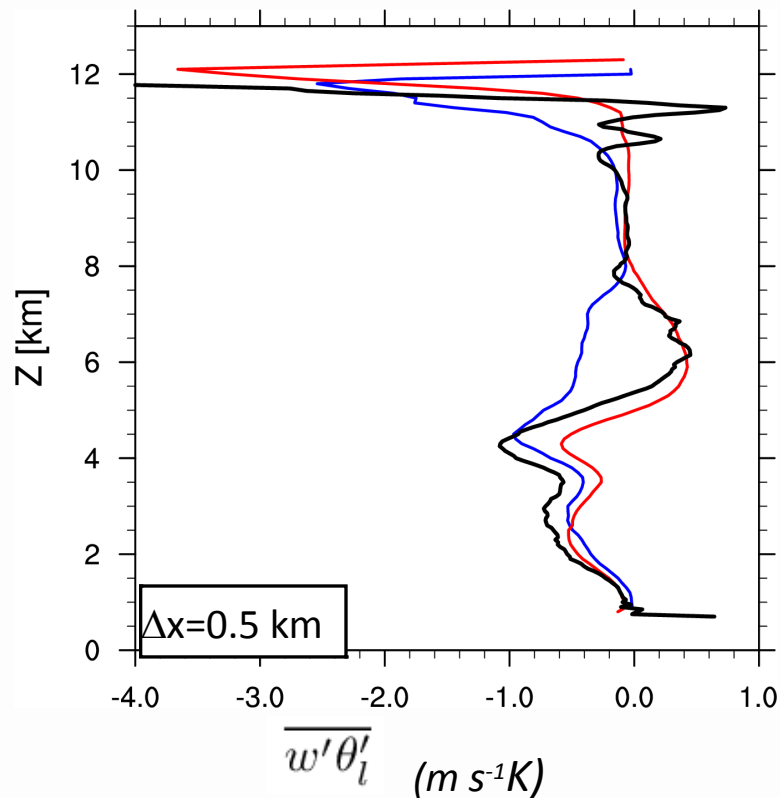


- more TKE and weaker W for **Hgrad** compared to **Kgrad**
- better balance between subgrid and resolved parts

3 – Evaluation of turbulence parameterization

On-line evaluation: simulations **with $\Delta x = 0.5$ km, 2 km**

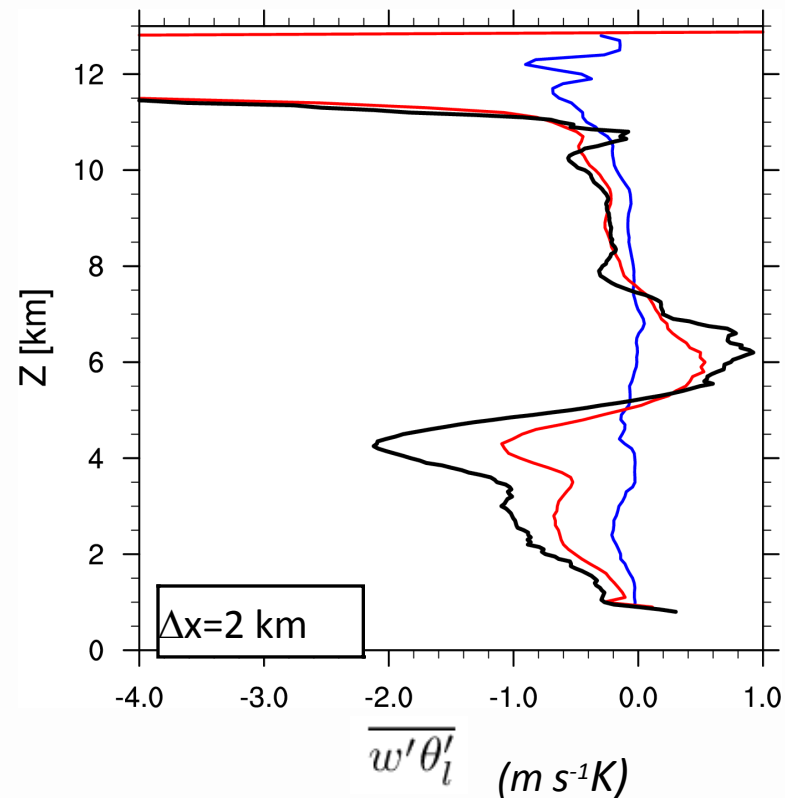
Vertical profiles inside convective system $t = 180$ min



REF (LES)

Kgrad

Hgrad



→ positive impact at 0.5 km and 2 km

- **Characterization of turbulence from a reference LES:**
 - strong TKE inside convective clouds, subgrid TKE increases with coarser resolutions, thermal production increases whereas dynamical production decreases
 - anisotropy increases with coarser resolutions
 - counter-gradient areas for turbulent fluxes due to coherent structures → non-local turbulence
- **Evaluation of turbulence parameterization inside convective clouds**
 - K-gradient formulation not suitable: too weak subgrid TKE and too strong W as shown in *Verrelle et al., 2015, QJRMS*
 - better representation with a parameterization based on horizontal gradients (*Moeng et al, 2010*):
 - better vertical turbulent fluxes of heat and water mixing ratio
 - better balance between subgrid and resolved parts
→ *Verrelle et al., Submitted to MWR*

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→ Next step:

Evaluation of the new parameterization on real convective cases from HyMeX

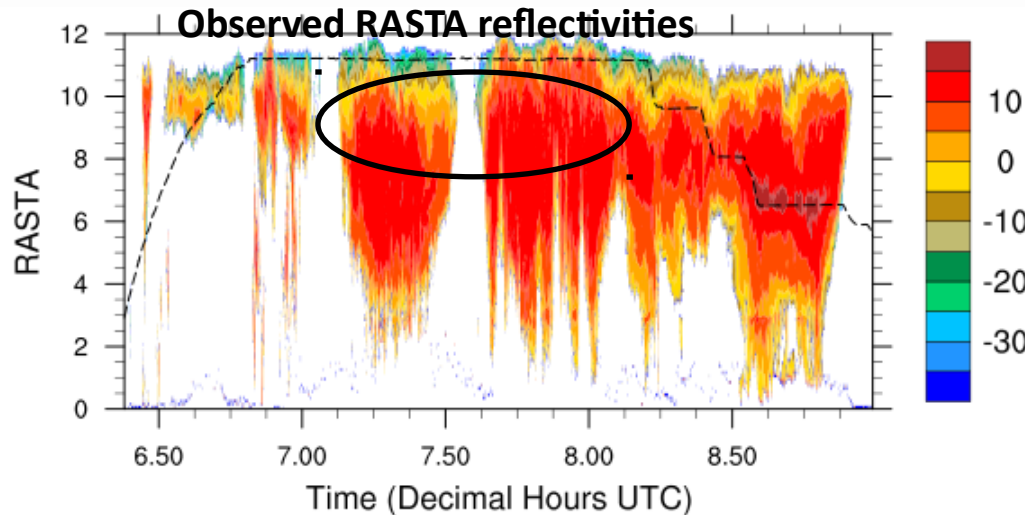
- at different horizontal resolutions (500m, 1km, 2km)
- validation with comparison to observational datasets



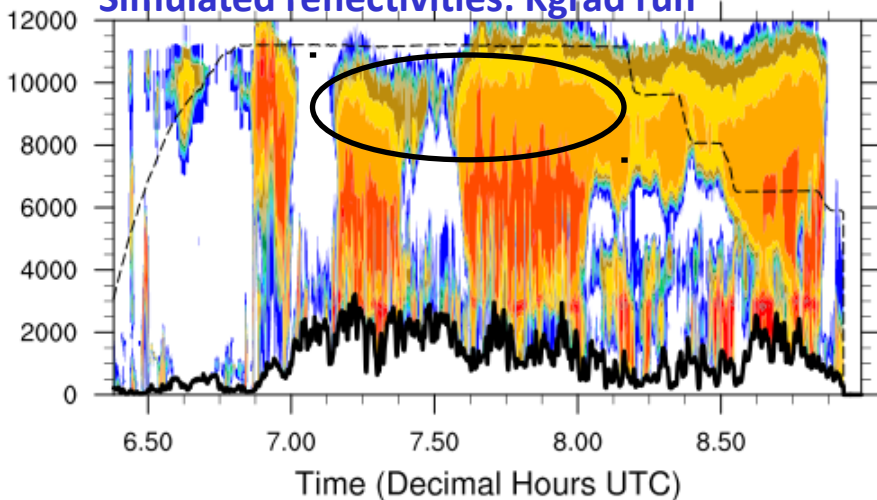
Conclusion

Radar reflectivities along Falcon-20 trajectory (dBZ) during IOP6 (24 september 2012)

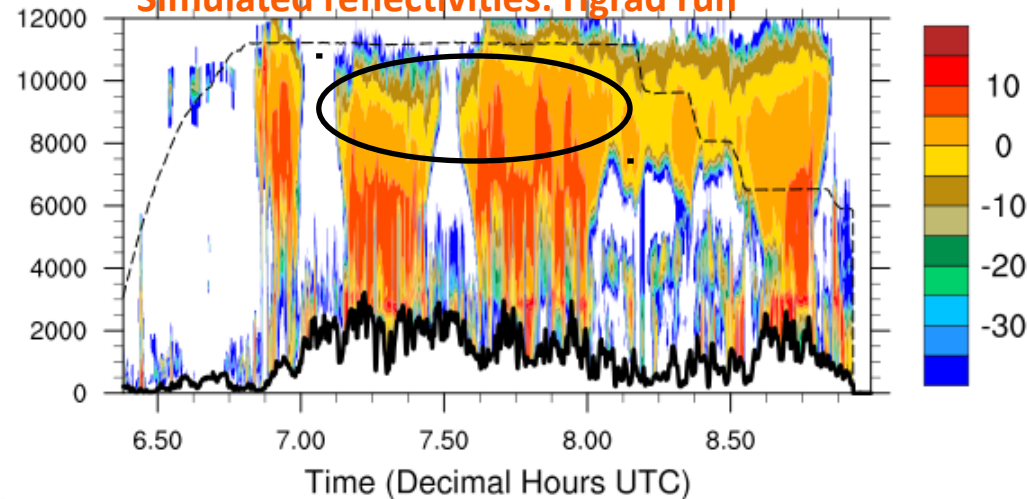
Post-doc: Nicolas Rochetin



Simulated reflectivities: Kgrad run



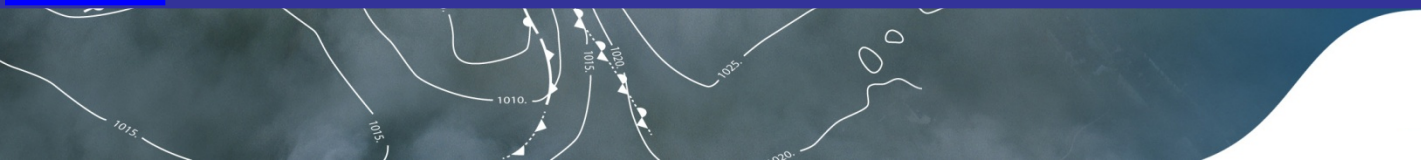
Simulated reflectivities: Hgrad run



→ Preliminary results: higher reflectivities in the upper part of the clouds with Hgrad due to more ice, snow and graupel



Thank you for your attention!



3 – Evaluation of turbulence parameterization

Tensor: decomposed in 3 terms

$$\tau_{ws} = \underbrace{\left[\widetilde{\widetilde{ws}} - \widetilde{\widetilde{ws}} \right]}_L + \underbrace{\left[\widetilde{ws'} + \widetilde{w's} - \widetilde{\widetilde{ws'}} - \widetilde{\widetilde{w's}} \right]}_C + \underbrace{\left[\widetilde{w's'} - \widetilde{\widetilde{w's'}} \right]}_R$$

L Leonard term
(filtered variables)

C Cross term
(interaction)

R Reynolds term
(fluctuations)

$$L_{ws} = \widetilde{\widetilde{ws}} - \widetilde{\widetilde{ws}} = \left(\frac{\Delta x^2}{12} \right) \left(\frac{\partial \widetilde{w}}{\partial x} \frac{\partial \widetilde{s}}{\partial x} + \frac{\partial \widetilde{w}}{\partial y} \frac{\partial \widetilde{s}}{\partial y} \right)$$

Bardina et al, 1980,
Clark et al 1979,
Chow et al, 2005

Limited
development

Moeng et al, 2010:

$$\tau_{ws} = \underbrace{L_{ws}}_L + \underbrace{C_{ws}}_C + \underbrace{R_{ws}}_R = 2 \left(\frac{\Delta x^2}{12} \right) \left(\frac{\partial \widetilde{w}}{\partial x} \frac{\partial \widetilde{s}}{\partial x} + \frac{\partial \widetilde{w}}{\partial y} \frac{\partial \widetilde{s}}{\partial y} \right) - \underbrace{K \frac{\partial \widetilde{s}}{\partial z}}_R$$

Mixte model

Moeng, 2014:

$$\overline{w's'} = \underbrace{A_1 (w^u - w^d)(s^u - s^d)}_{\text{mass flux}} \quad \overline{w's'} = A_1 A_2 \left(\frac{\partial \overline{w}}{\partial x} \frac{\partial \overline{s}}{\partial x} + \frac{\partial \overline{w}}{\partial y} \frac{\partial \overline{s}}{\partial y} \right)$$

3 – Evaluation of turbulence parameterization

Off-line evaluation: computation of parameterized fluxes from LES at $\Delta x \rightarrow \overline{w'\theta'_l}$

CTRL

Cuxart et al (2000)

$$\overline{w'\theta'_l}^{\Delta x} = -\frac{2}{3C_{p\theta}} \overline{\phi_i}^{\Delta x} L \sqrt{\overline{e}_{ref}^{\Delta x}} \frac{\partial \overline{\theta_l}^{\Delta x}}{\partial z}$$

based on K-gradient: $\overline{w'\theta'_l} = -K \frac{\partial \overline{\theta_l}}{\partial z}$

TEST1

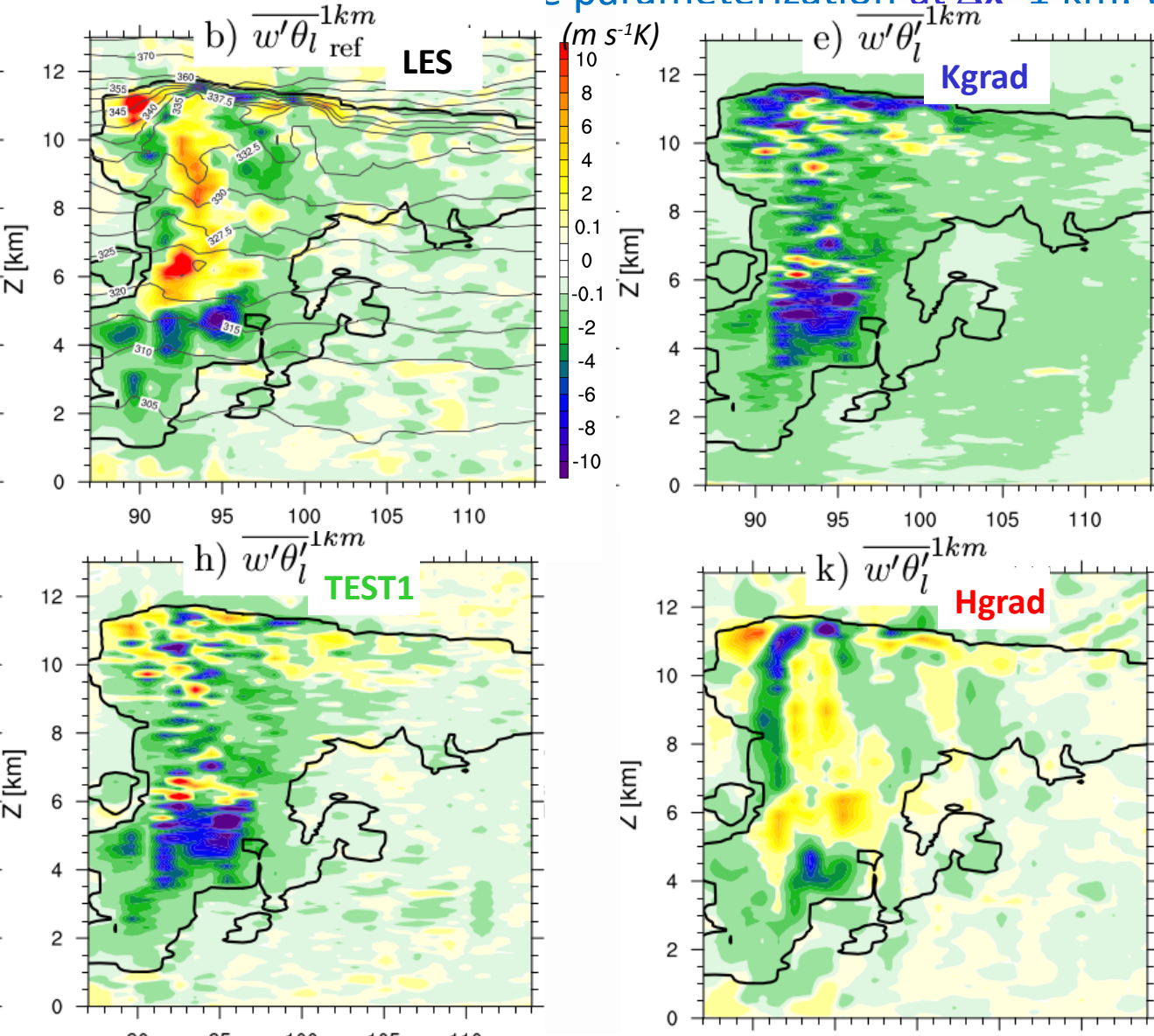
Zilitinkevich et al (1999)

$$\overline{w'\theta'_l}^{\Delta x} = -\frac{L}{C_{p\theta} \sqrt{\overline{e}_{ref}^{\Delta x}}} \left[\overline{w'^2}^{\Delta x} \frac{\partial \overline{\theta_l}^{\Delta x}}{\partial z} - \frac{2}{3} \beta (E_{\theta} \overline{\theta_l'^2}^{\Delta x} + E_r \overline{\theta_l' r'_{np}}^{\Delta x}) \right]$$

based on K-gradient with a counter-gradient term: $\overline{w'\theta'_l} = -K \left(\frac{\partial \overline{\theta_l}}{\partial z} - \gamma \right)$

Characterization of turbulence inside convective clouds

Evaluation of turbulence parameterization at $\Delta x=1$ km: vertical heat flux



→ positive flux inside the cloud
→ Better representation with horizontal gradient formulation

$\Delta x=1$ km