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Is there a need for local horizontal discretizations?

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- What's wrong with a spectral model?
- What can local methods bring us, and at what price?
- Conclusions and prospects





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In fact, our goal is pretty simple: develop the best possible atmospheric model. (and have fun while doing so)



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... but what does best mean?

Compromises are necessary (e.g. accuracy vs. cpu time)



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... but what does best mean?

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Currently, our model uses a spectral horizontal discretization. Are we confronting the limitations of spectral methods? What trade-off is made by local methods?



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... but what does best mean?

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- Currently, our model uses a spectral horizontal discretization.
 Are we confronting the limitations of spectral methods? What trade-off is made by local methods?
- Spoiler alert: no definitive answers will be given in this presentation!



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From the accuracy point of view, spectral methods are unsurpassable: their order of accuracy is infinite!

- (Limited tests indicate that) even over steep slopes, the accuracy of spectral methods remains unchallenged.
- Moreover, the calculation of derivatives and solving the Helmholz equation are trivial. This allows for (semi-)implicit timestepping and large timesteps. So our spectral dynamics are also quite *efficient*.



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- From the accuracy point of view, spectral methods are unsurpassable: their order of accuracy is infinite!
- (Limited tests indicate that) even over steep slopes, the accuracy of spectral methods remains unchallenged.
- Moreover, the calculation of derivatives and solving the Helmholz equation are trivial. This allows for (semi-)implicit timestepping and large timesteps. So our spectral dynamics are also quite *efficient*.
- ... but they require spectral transforms (FFT or Legendre transform for the global).
 These are nonlocal, i.e. they require domain-wide communication.
 This makes their use problematic on massively parallel machines.
- (another disadvantage of a spectral model is the requirement of a homogeneous reference state for the semi-implicit timestepping)
- But at what point do the costs no longer justify the accuracy?
 - to answer this question, we must closely investigate the alternatives.



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When considering alternatives for the spectral horizontal discretization, we try to keep as much as possible of the model intact:

- only way to make a clean comparison
- limited development cost (no need to modify physics, ...)

So for the time being, we stick to a semi-implicit time discretization and a semi-Lagrangian advection scheme.



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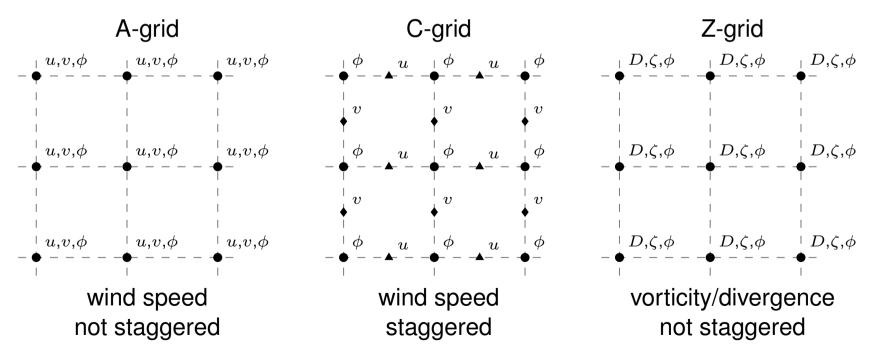
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- limited development cost (no need to modify physics, ...)

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Finite-difference discretizations are considered on the following grids:



These discretizations are tested with a 1D shallow water toy model.





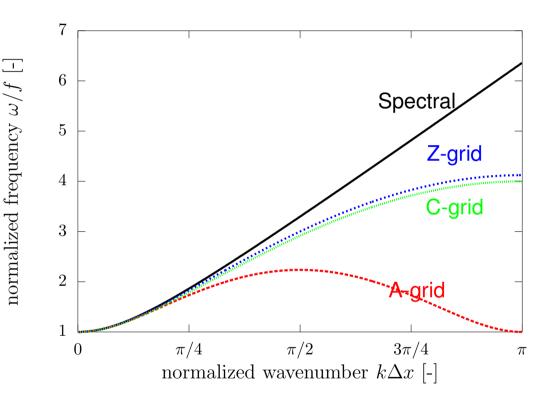
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It is well known (Mesinger & Arakawa, 1976) that the dispersion relation of gravity waves on an A-grid is problematic (negative group velocity at the shortest scales).

- The C-grid doesn't have this problem, but the staggering makes semi-Lagrangian advection 3 times more expensive.
- Pierre Bénard has shown (cfr. Piet's presentation of last year) that in certain cases, the short waves behave better on an Agrid than on a C-grid.
- Z-grid seems to offer the best of both worlds (at the expense of solving a Poisson equation to retrieve wind from vorticity/divergence), if timesymmetry is respected.



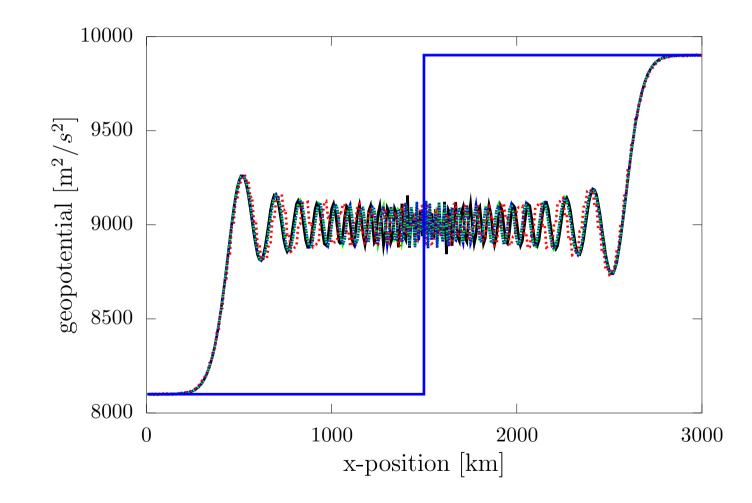


Checking the geopotential behavior for a geostrophic adjustment problem seems to confirm this

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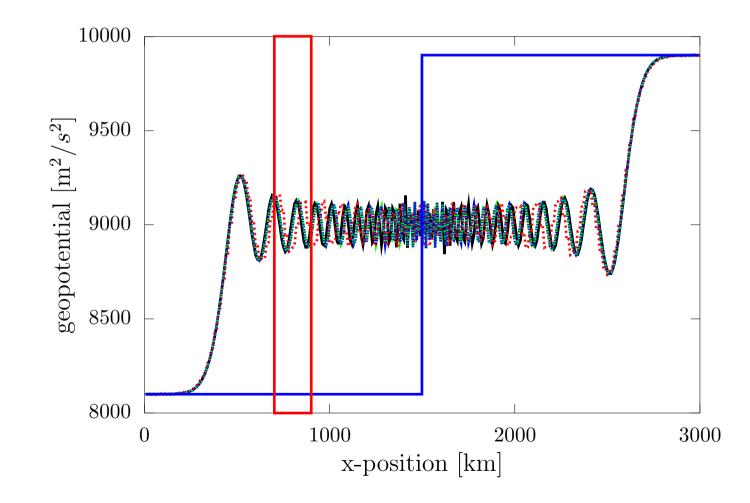


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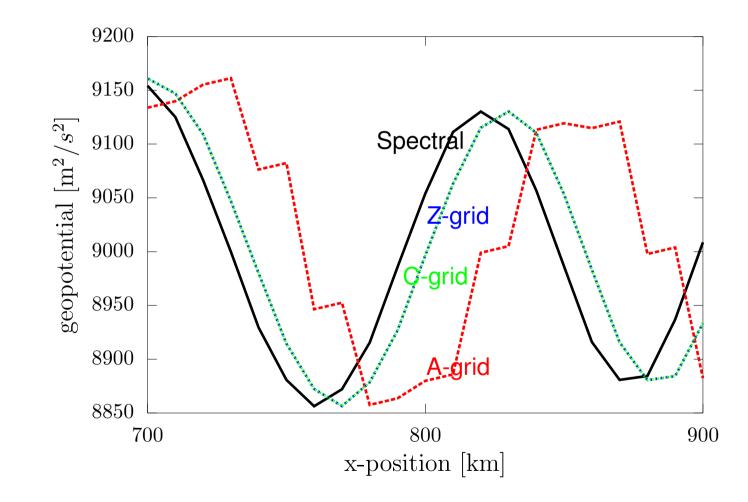


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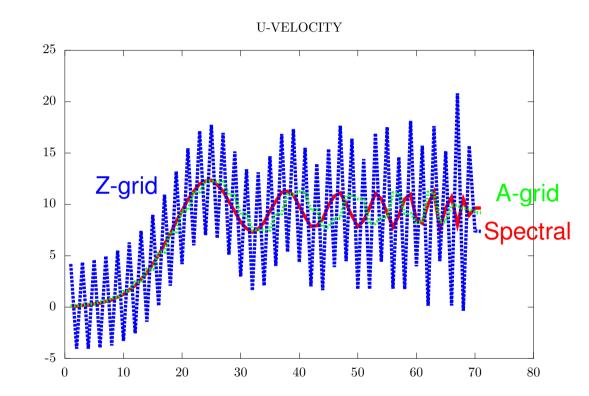
strange is observed.

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Already after a single timestep, the *u*-field turns out to be very noisy!



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Z-grid adjustment test

What's happening here? We'll do the analysis for a simpler SWE system without Coriolis terms.

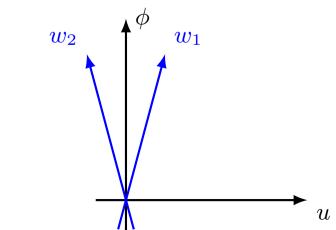
The (linearized) SWE are a hyperbolic system. The solution is dominated by two waves.

These waves (w_1, w_2) are a combination of the prognostic variables (u, ϕ) , and can be seen as 'more fundamental' solutions since they propagate independently from one another.

The exact transformation between wave amplitudes and prognostic variables is not wavenumber dependent:

$$\left(\begin{array}{c} u\\ \phi\end{array}\right) = \left(\begin{array}{cc} 1 & -1\\ c & c\end{array}\right) \left(\begin{array}{c} w_1\\ w_2\end{array}\right)$$

with $c \sim 100 \, \mathrm{m/s}$



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- In the discrete case, the transformation is determined by the *eigenvectors* of the amplification matrix (while the dispersion relation is determined by the eigenvalues).
- For a spectral, A-grid and C-grid discretization, the wavenumber-independence is retained.



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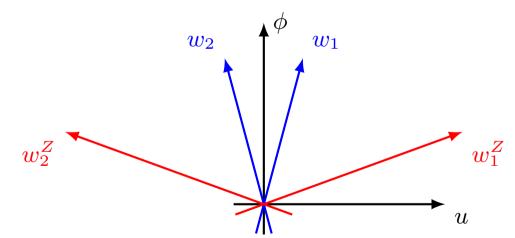
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Z-grid adjustment test

- For a spectral, A-grid and C-grid discretization, the wavenumber-independence is retained.
- But for the Z-grid discretization, the transformation becomes wavenumberdependent:

$$\begin{pmatrix} u \\ \phi \end{pmatrix} = \begin{pmatrix} \sqrt{2 - 2\cos k\Delta x} & -\sqrt{2 - 2\cos k\Delta x} \\ c\sin k\Delta x & c\sin k\Delta x \end{pmatrix} \begin{pmatrix} w_1 \\ w_2 \end{pmatrix}$$

For the shortest waves $(k\Delta x \rightarrow \pi)$, the ϕ -component becomes relatively small:





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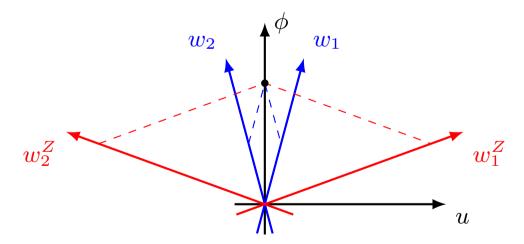
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As a consequence, an initial state without *u*-component is decomposed into two waves with non-negligible (but initially opposite) *u*-component.

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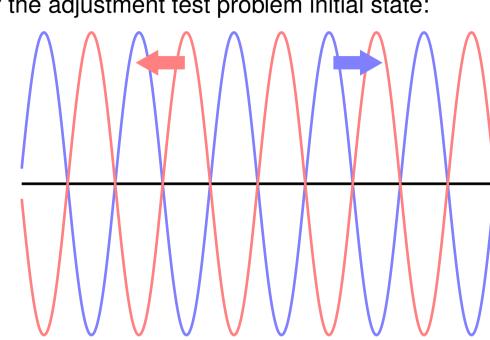
Decomposition of the adjustment test problem initial state:

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The two gravity waves propagate in opposite directions, and after a single timestep, this results in a noisy *u*-field.



Conclusions from these tests

What we've seen so far:

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- Every discretization has its strengths and weaknesses.
- The quality of a discretization is case-dependent (advection vs. adjustment).
- The discretization effects may be very subtle. Even careful inspection of the dispersion relation (eigenvalues) is no guarantee to have proper behavior.



Conclusions from these tests

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- The discretization effects may be very subtle. Even careful inspection of the dispersion relation (eigenvalues) is no guarantee to have proper behavior.
- To make these conclusions even more relative: how representative is the shallow water toy model for a 3D atmospheric model?
 - diabatic effects triggering shortest waves
 - numerical diffusion filtering shortest waves



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- To make these conclusions even more relative: how representative is the shallow water toy model for a 3D atmospheric model?
 - diabatic effects triggering shortest waves
 - numerical diffusion filtering shortest waves
 - And that's not the end yet. The most suitable discretization also depends on the (future!) hardware:
 - efficiency
 - scalability (in fact the main motivation for reviewing the spectral dynamical core)
 - energy consumption

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What we've seen so far:

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- To make these conclusions even more relative: how representative is the shallow water toy model for a 3D atmospheric model?
 - diabatic effects triggering shortest waves
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 - And that's not the end yet. The most suitable discretization also depends on the (future!) hardware:
 - efficiency
 - scalability (in fact the main motivation for reviewing the spectral dynamical core)
 - energy consumption
 - So the 'best' solution is very much situation dependent.

The only way out of this situation is to aim for a *modular* code, where different options can be used next to each other.



The ESCAPE project

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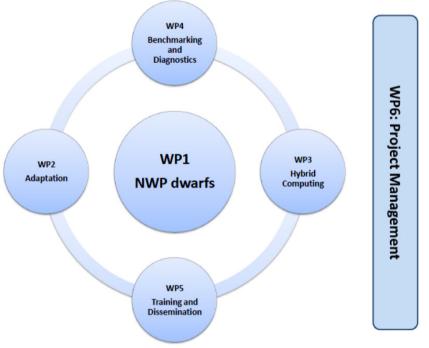
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The ESCAPE project was recently approved for H2020 EU funding.

ECMWF is the coordinating partner; other partners include HIRLAM and ALADIN members, HPC hardware manufacturers, universities and supercomputing centers.

- The core of ESCAPE is the identification of fundamental algorithm building blocks ('NWP dwarfs'), e.g.
 - spectral transforms
 - sparse solvers
 - unstructured mesh generation
 - advective transport mechanisms
 - time-stepping strategies
 - . . .



- Adaptation of NWP dwarfs to hardware accelerators
- Benchmarking strategies to gauge code efficiency and energy consumption on heterogeneous hardware
- Breakdown of the model in these dwarfs means modularity

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Thank you !